

# Characteristics of the rotor R4-07 for the O4 NCal system VIR-0861B-22

Eddy Dangelser, Dimitri Estevez, Benoit Mours,  
Mehmet Ozturk, Antoine Syx

IPHC-Strasbourg

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This note is a revised version of the previous release. On June 12, 2023 this rotor was machined at IPHC to flatten the surface of the upper sectors.

## 1 Introduction

This note follows the same discussion made on the rotor R4-01 in [VIR-0591C-22](#) and R4-05 in [VIR-0859A-22](#). The drawings and figures of the rotor can be found in this first technical note.

The rotor has been engraved IPHC-R4-07 on one side and sandblasted on the other side.

## 2 Measurement method

To determine the geometry of the rotor we will use the same method as for R4-01 (see [VIR-0591C-22](#)). The thickness was measured using  $24 \times 2 = 48$  points (see fig. 1), the outer diameter was measured in  $4 \times 2 = 8$  points and the inner diameter using 4 points.

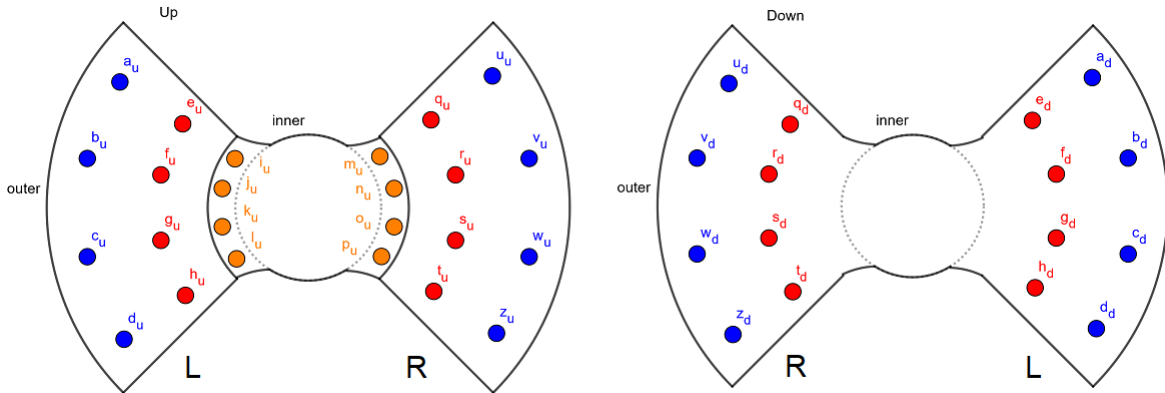


Figure 1: Outline of the faces of the rotor with the measurement points. Left figure is face up, right figure is face down. Sectors have been labelled L for left sector and R for right sector.

The tool used to measure the thickness and the outer diameter is a measuring column "Garant 44 5350\_600 HC1" (see [VIR-0160A-22](#)) with a given precision of  $1.8 + L/600 \mu\text{m}$  (L the measured length in mm). A vernier caliper "TESA-CAL IP67" with a precision of  $20 \mu\text{m}$  was used to measure the inner diameter.

The measuring column was operated on a metrology table with a value range from 0 to  $2 \mu\text{m}$ . The rms of the 16 values is  $0.9 \mu\text{m}$ .

We measured the opening angles of the sectors using a video measuring microscope "Garant MM2" (see [VIR-0591C-22](#)) with a given precision of  $2.9 + L/100 \mu\text{m}$  at 95% CL (L the measured length in mm).

### 2.1 Thermal effects and density

The rotor R4-07 has been machined from the same aluminum block as R4-05 described in [VIR-0859A-22](#). As for R4-05 the results will be expressed at a reference temperature of  $23^\circ\text{C}$ .

The density of the rotor R4-07 is then  $2810.8 \pm 0.2 \text{ kg}\cdot\text{m}^{-3}$ . This density is measured in air, if the rotor is used under vacuum, the density should be increased by the air density ( $\rho_{air} = 1.3 \text{ kg}\cdot\text{m}^{-3}$ ).

### 3 Raw measurements of the rotor

This section presents the raw measurements made on the rotor at the ambient temperature of 25.4 °C for the heights and 24.5°C for the diameters. Table 1 shows the thickness measurements according to the measurement points defined in figure 1. The rotor is laying on the table. The rotor surface as well as the table are not perfectly flat. Some space could be present in between that should be subtracted when computing the rotor thickness as discussed later.

Measurement point	L sector		Measurement point	R sector	
	Up	Down		Up	Down
a	104.349	104.353	q	104.348	104.355
b	104.364	104.364	r	104.341	104.354
c	104.361	104.371	s	104.343	104.356
d	104.346	104.373	t	104.351	104.362
e	104.357	104.371	u	104.337	104.331
f	104.372	104.374	v	104.346	104.334
g	104.376	104.378	w	104.353	104.340
h	104.371	104.381	z	104.351	104.343
i	101.502		m	101.499	
j	101.499		n	101.497	
k	101.497		o	101.494	
l	101.498		p	101.496	

Table 1: Raw measurements of the height in mm for each point at 25.4°C on L and R sectors of R4-07.

Table 2 displays the diameter measurements. The measurements were made on 4\*2 diameters (two parts of each diameter, the up and down sides of the rotor).

Measurement point	Up	Down
1	207.974	207.957
2	207.987	207.984
3	207.985	207.985
4	207.950	207.958

Table 2: Raw measurements of the diameter in mm for each point at 24.5°C on R4-07.

Theoretical values were taken for the inner radius  $r_{\min} = 29$  mm and the up face radius for the counterweight  $r_{\text{counterweight}} = 40$  mm (see drawing in [VIR-0591C-22](#)).

## 4 Extracting the geometrical parameters

### 4.1 Thickness

We need to correct the possible gap between the rotor and the measuring table. Assuming that the table is flatter than the rotor surface we can extract the gap from the measurement of the top surface considering the plane tangents to the highest points (asking them to be on both sectors). For this rotor these points are f, g, w for the up and g, h, t for the down face (see fig. 1). Using the measurements in table 1 we can compute a plane equation for each side of the rotor in cartesian coordinates:

$$\text{Up plane equation : } z = -1.72 \times 10^{-4}x - 1.82 \times 10^{-4}y + 104.36 \quad (1)$$

$$\text{Down plane equation : } z = -2.02 \times 10^{-4}x - 2.34 \times 10^{-4}y + 104.36 \quad (2)$$

Using eqs. (1) and (2) the gap can be determined, see table 3. The maximum rms of the gap for each sector is 12  $\mu\text{m}$ .

Measurement point	L sector		Measurement point	R sector	
	Up	Down		Up	Down
a	19	15	q	3	-7
b	12	14	r	12	-3
c	22	15	s	14	0
d	40	17	t	11	0
e	10	-5	u	6	7
f	0	-1	v	1	9
g	0	0	w	0	11
h	7	0	z	10	18

Table 3: Gap computed in  $\mu\text{m}$  on up and down sides of both sectors of R4-07.

We can then compute the rotor thickness for each point by removing these gaps. If one of the raw values is lower than the corrected thickness we take this lowest value. The value of each point is shown in table 4 at 23°C.

Measurement point	L sector	Measurement point	R sector
a	104.399	q	104.409
b	104.384	r	104.399
c	104.363	s	104.385
d	104.343	t	104.379
e	104.403	u	104.402
f	104.393	v	104.390
g	104.383	w	104.385
h	104.378	z	104.379
i	101.498	m	101.495
j	101.497	n	101.493
k	101.494	o	101.491
l	101.495	p	101.492

Table 4: Measurements of the thickness in mm for each point at 23°C on L and R sectors of R4-07.

## 4.2 Radius

Using comparators while the rotor is rotating on its axis we can determine the deformation on both sectors and compute different radii values. Table 5 shows the raw measurements using comparators on L and R sectors. The measurements were made on the up, center and down sides of L and R sectors using three comparators for a total of  $5 \times 3 \times 2 = 30$  points (the first and last points are near the edge of the sectors).

Measurement point	L sector			R sector		
	Up	Center	Down	Up	Center	Down
A	10	0	-10	-10	-10	0
B	30	35	45	30	30	35
C	40	45	50	40	45	40
D	30	35	35	35	30	30
E	0	0	0	0	-5	-5

Table 5: Raw measurements in  $\mu\text{m}$  of the comparators for the L and R sectors of R4-07.

The zeroing of the comparators was made arbitrarily close to the edge of the sector. The offsets shown in table 5 are measured relative to this reference.

To compute the radius per measurement point we use the following process: First we compute the mean deformation for one comparator. Then we remove this mean deformation to each measurement of this comparator. The corrected shift value is added to the mean radius of 103.983 mm computed using table 2 at 23°C. This process is repeated for each comparator. The final radius for each point are shown in table 6.

Measurement point	L sector			R sector		
	Up	Center	Down	Up	Center	Down
A	103.976	103.966	103.954	103.956	103.956	103.964
B	103.996	104.001	104.009	103.996	103.996	103.999
C	104.006	104.011	104.014	104.006	104.011	104.004
D	103.996	104.001	103.999	104.001	103.996	103.994
E	103.966	103.966	103.964	103.966	103.961	103.959

Table 6: Radius measurements in mm at 24.5°C for the L and R sectors of R4-07.

## 5 Characterization of the rotor using a simple model

### 5.1 Theoretical model of the rotor

As explained in VIR-0591C-22 the theoretical strain of the mirror at  $2f$  using FROMAGE v1r2 with the rotor design parameters:

$$\text{strain}(2f) = \frac{2.1217 \times 10^{-18}}{(2f_{rot})^2}$$

This strain value will be compared to models based on the measurements of the rotor.

### 5.2 Thickness

A simple model can be used to determine a mean value for the thickness and its uncertainty.

As shown on fig. 1, a total of 16 points were used to compute the thickness of each sector. In this case we will not consider the inner points so that we obtain uniform sectors.

For the simple model we take the thickness as the mean value of table 4: 104.345 mm at 23°C. Since we have a limited number of measurement points, to be conservative we take the thickness uncertainty as the rms of table 4 (14.0  $\mu\text{m}$ ) to which we add linearly the metrology table uncertainty (0.9  $\mu\text{m}$ ) and the tool uncertainty (2.0  $\mu\text{m}$ ). Therefore, for this simple model, the thickness is  $104.345 \pm 0.017$  mm.

### 5.3 Radius

For the simple model we take the radius as the mean value of table 6: 103.983 mm at 23°C. Using a linear sum of the rms of table 6 (20.4  $\mu\text{m}$ ) and the tool uncertainty (2.2  $\mu\text{m}$ ) we take an uncertainty of 23  $\mu\text{m}$  on the mean radius.

We have to point out that we do not take into account the fact that the sectors might not be centered on the same axis. Therefore the uncertainty might be underestimated. We will then consider each sector individually later.

### 5.4 Expected NCal signal and uncertainties

The geometry used to describe the rotor as a simple model is represented in figure 2.

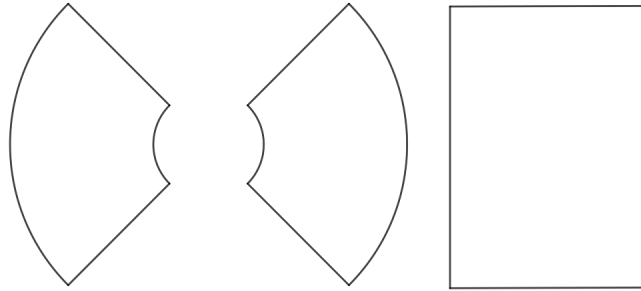


Figure 2: Simple model geometry used to describe the rotor. Left is a front view, right is a side view.

Using the analytical equation of the strain at 2f (see eq.8 in [Newtonian calibrator tests during the Virgo O3 data taking](#)) we compute with our parameters ( $d = 1.7$  m and an angle  $\phi = 34.7^\circ$ ):

$$\text{strain}(2f) = \frac{2.1192 \times 10^{-18}}{(2f_{rot})^2}.$$

Using FROMAGE on this geometry we compute the following 2f strain on the mirror at a distance of 1.7m and an angle of 34.7°:

$$\text{strain}(2f) = \frac{2.1193 \times 10^{-18}}{(2f_{rot})^2}$$

Comparing the theoretical model strain with the simple model at 2f using FROMAGE we obtain a relative deviation of 0.118%.

Comparing the analytical strain at 2f with FROMAGE we obtain a relative deviation of 0.005%.

The uncertainties considered for this model are displayed in table 7.

R4-07 rotor parameter simple model (23°C)			NCal 2f signal uncertainty	
name	value	uncertainty	formula	value (%)
Density $\rho$ (kg.m <sup>-3</sup> )	2810.8	0.2	$\delta\rho/\rho$	0.007
Thickness $b$ (mm)	104.345	$1.7 \times 10^{-2}$	$\delta b/b$	0.016
$r_{max}$ (mm)	103.983	$2.3 \times 10^{-2}$	$4\delta r_{max}/r_{max}$	0.087
$G$ (m <sup>3</sup> .kg <sup>-1</sup> .s <sup>-2</sup> )	$6.67430 \times 10^{-11}$	$1.5 \times 10^{-15}$	$\delta G/G$	0.002
Temperature $T$ (°C)	23	3	$\frac{\partial h}{\partial T} \frac{\Delta T}{h}$	0.014
Quadratic sum				0.090

Table 7: Uncertainties on the amplitude of the calibration signal at 2f from the R4-07 rotor simple model geometry..

## 6 Characterization of the rotor using an advanced model

### 6.1 Thickness

A more advanced model can be used considering the deformations on the surfaces of the sectors for better accuracy. Each measurement point of table 4 can be considered as a sub-sector with its own thickness.

The uncertainty on this value is more complex to evaluate. As a conservative approach we use the maximum rms of the deviation to a plane for each sector (12  $\mu\text{m}$  see section 4.1) to which we add linearly the uncertainty on the flatness of the measurement table (0.9  $\mu\text{m}$ ) as well as the measurement tool (2.0  $\mu\text{m}$ ). The total uncertainty on the thickness is 16  $\mu\text{m}$ .

### 6.2 Radius

On fig. 1 we divided the external sectors in 4 sub-sectors for each sector (blue points). We convert the point of table 6 to the grid of fig. 1 by averaging the two closest values and converting them to 23°C. The results are shown in table 8. We notice that the L sector is on average 3  $\mu\text{m}$  larger than the R sector.

Radius	L sector			R sector		
	Up	Center	Down	Up	Center	Down
1	103.982	103.980	103.978	103.972	103.972	103.978
2	103.997	104.002	104.008	103.997	104.000	103.998
3	103.997	104.002	104.003	104.000	104.000	103.996
4	103.977	103.980	103.978	103.980	103.975	103.973

Table 8: Radius measurements (in mm at 23°C) for the L and R sectors of R4-07.

The maximum rms of the radii for each sector is 12.2  $\mu\text{m}$ . The tool uncertainty is 2.2  $\mu\text{m}$ . Like for the thickness we use a linear sum and find the uncertainty on both radii to be 14  $\mu\text{m}$ .

### 6.3 Counterweight

A counterweight has been designed to reduce the unbalance of the rotor using the same method as R4-06 in section 6.3 of VIR-0860B-22. This counterweight is made of aluminum 2017 ( $\rho_{\text{Al}_{2017}} = 2790 \text{ kg.m}^{-3}$ ) and the geometry is shown in fig. 3.

The dimensions of the counterweight are: an inner radius of 10 mm, an outer radius of 40 mm and a material cut with a chord of 65.22 mm to balance the rotor (see hatched are on fig. 3).

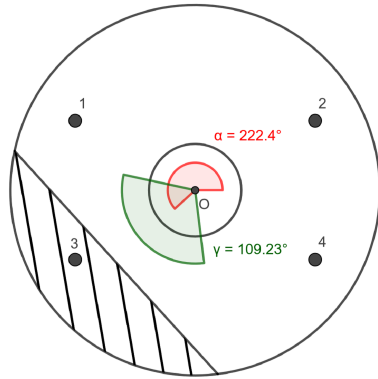


Figure 3: Outline of the counterweight for R4-07. The hatched area represents the material removed.

## 6.4 Opening angles and asymmetry

The opening angles of the full and empty sectors have been measured using a video microscope with the same method as for R4-01. The uncertainty on  $\alpha = 0.2$  mrad is the same as for R4-01 giving an uncertainty of  $4 \times 10^{-6}$  % on the  $2f$  signal which is neglectable.

The measurements are shown in table 9. The center value corresponds to the mean of up and down measurements.

Opening angle	Up	Center	Down
L	1.57084	1.57078	1.57073
R	1.57058	1.57066	1.57074
L-R	1.57096	1.57104	1.57112
R-L	1.57080	1.57069	1.57059

Table 9: Opening angle measurements in rad for the L, R full sectors and L-R, R-L empty sectors of R4-07.

These measurements allow us to compute the signal with different opening angles and an asymmetry between the sectors. These measured opening angles will be included in the advanced model described in the next section.

## 6.5 Expected NCal signals and uncertainties

### 6.5.1 Advanced geometry including chamfers and counterweight

The geometry used to describe the rotor as an advanced model is represented in figure 4. The external parts of the sectors are divided in 3 sub-sectors each to correspond to the different radii determined. In addition we include the counterweight, the screws, the screw holes, the opening angles and asymmetry of the sectors.



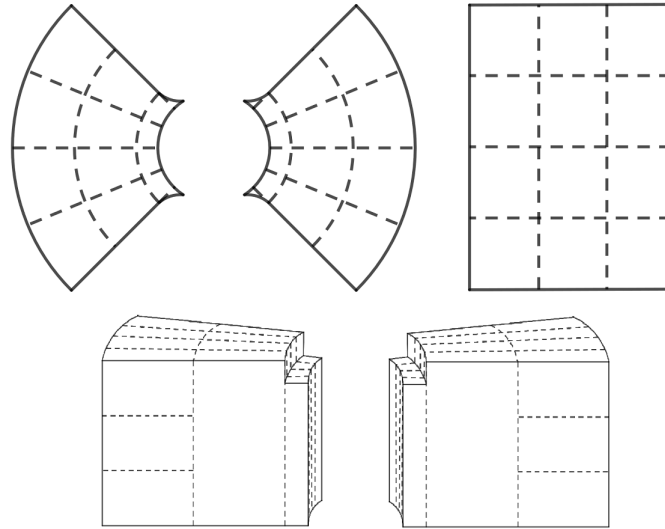


Figure 4: Advanced model geometry used to describe the rotor. Top left is a front view, top right is a side view (external sub-sectors) and bottom is a tilted view of the sectors. Only the 4 external part sectors are divided in 3 sub-sectors each. The chamfers are visible on the inner radius.

Using FROMAGE on this geometry gives the following strains:

- $\text{strain}(1f) = \frac{2.3788 \times 10^{-20}}{(1f_{rot})^2}$
- $\text{strain}(2f) = \frac{2.1186 \times 10^{-18}}{(2f_{rot})^2}$
- $\text{strain}(3f) = \frac{2.9178 \times 10^{-23}}{(3f_{rot})^2}$

The relative deviation to the simple model at 2f is 0.033%.

### 6.5.2 Remaining geometry uncertainty

Since R4-02 and following have been machined with a better precision than R4-01 as seen from the lower 1f value. The remaining geometry uncertainties are taking as for R4-01.

### 6.5.3 Uncertainties

To set an uncertainty on the strain(2f) from the description of the geometry we take the difference between the simple model ( $\text{strain}(2f) = 2.1193 \times 10^{-18}/(2f)^2$ ) and the advanced model ( $\text{strain}(2f) = 2.1186 \times 10^{-18}/(2f)^2$ ). This deviation, 0.033%, is reported in table 10 as modelling uncertainty.

The uncertainties considered for this full model are displayed in table 10.

R4-07 rotor parameter advanced model (23°C)			NCal 2f signal uncertainty	
name	mean value	uncertainty	formula	value (%)
Density $\rho$ (kg.m <sup>-3</sup> )	2810.8	0.2	$\delta\rho/\rho$	0.007
Thickness $b$ left sector (12 sub-sectors) (mm)	104.355	$1.6 \times 10^{-2}$	$\delta b/b$	0.015
Thickness $b$ right sector (12 sub-sectors) (mm)	104.334			
$r_{max}$ left sector (12 ext sub-sectors) (mm)	103.990	$1.4 \times 10^{-2}$	$4\delta r_{max}/r_{max}$	0.055
$r_{max}$ right sector (12 ext sub-sectors) (mm)	103.987			
$G$ (m <sup>3</sup> .kg <sup>-1</sup> .s <sup>-2</sup> )	$6.67430 \times 10^{-11}$	$1.5 \times 10^{-15}$	$\delta G/G$	0.002
Temperature $T$ (°C)	23	3	$\left  \frac{\partial h}{\partial T} \right  \frac{\Delta T}{h}$	0.014
Modelling Uncertainty				0.033
FROMAGE grid uncertainty				0.005
Opening angle and sector asymmetry uncertainty				$< 5 \times 10^{-4}$
Remaining geometry uncertainty				$< 5 \times 10^{-4}$
Total uncertainty from the rotor (quadratic sum)				0.068

Table 10: Uncertainties on the amplitude of the calibration signal at 2f from the R4-07 rotor advanced model geometry at 23°C.

## A Appendix

```
### This is a cfg file for a more realistic geometry of the mirror and the Virgo NCal R4-07 (2022)
```

```
### ALL THE OBJECTS ARE DEFINED IN THE MIRROR'S FRAME (0,x,y,z),
### with 0 the center of the mirror, x axis along the ITF's beam toward the beam-splitter,
### y axis orthogonal to x in the plane of the ITF,
### z axis orthogonal to the plane of the ITF upward
```

```
### MIRROR DEFINITION
```

```
GRID_SIZE 12 30 8
```

```
CYLINDER 2202. 0 0.175 0.2 360 0 0 0
```

```
GRID_SIZE 1 1 1
```

```
# Defining the flats on the edge of the mirror
```

```
CUT_CYL 2202. 0.175 0.2 0.05 0 0
```

```
CUT_CYL 2202. 0.175 0.2 0.05 0 180
```

```
# Defining the ears and anchors of the mirror
```

```
CUBOID 2202. 0.090 0.010 0.015 0 0.1782 -0.0125
```

```
CUBOID 2202. 0.090 0.010 0.015 0 -0.1782 -0.0125
```

```
CUBOID 2202. 0.039 0.008 0.008 -0.02 -0.1772 -0.024
```

```
CUBOID 2202. 0.039 0.008 0.008 -0.02 0.1772 -0.024
```

```
CUBOID 2202. 0.039 0.008 0.008 0.02 -0.1772 -0.024
```

```
CUBOID 2202. 0.039 0.008 0.008 0.02 0.1772 -0.024
```

```
### ROTOR DEFINITION: CYLINDER DENSITY INNER_RADIUS OUTER_RADIUS THICKNESS OPEN_ANGLE r z theta
```

```
ROTOR_CYLINDRICAL 1.7 34.7 0 0
```

```
### COUNTERWEIGHT 2790.
```

```
GRID_SIZE 16 65 40
```

```
CYLINDER 2790. 0.010 0.040 0.003 360 0 0.0478828391032846 0
```

```
GRID_SIZE 1 1 1
```

```
CUT_CYL 2790. 0.040 0.003 0.06522 0.0478828391032846 222.4
```

```
### SCREW HOLES
```

```
GRID_SIZE 1 1 1
```

```
CYLINDER -2810.8 0 0.0015 0.012 360 0.03 0.04474812546 150
```

```
CYLINDER -2810.8 0 0.0015 0.012 360 0.03 0.04474612558 30
```

```
CYLINDER -2810.8 0 0.0015 0.012 360 0.03 0.04474662555 210
```

```
CYLINDER -2810.8 0 0.0015 0.012 360 0.03 0.04474512563 330
```

```
CYLINDER -2790. 0 0.0015 0.002 360 0.03 0.0478828391032846 150
```

```
CYLINDER -2790. 0 0.0015 0.002 360 0.03 0.0478828391032846 30
```

```
CYLINDER -2790. 0 0.0015 0.002 360 0.03 0.0478828391032846 210
```

```
CYLINDER -2790. 0 0.0015 0.002 360 0.03 0.0478828391032846 330
```

```
### SCREWS COUNTERWEIGHT
```

```
GRID_SIZE 1 1 1
```

```
CYLINDER 7600. 0 0.0015 0.00965 360 0.03 0.04305783910328 150
```

```
CYLINDER 7600. 0 0.0015 0.00965 360 0.03 0.04305783910328 30
```

```
CYLINDER 7600. 0 0.0015 0.00965 360 0.03 0.04305783910328 210
```

---

CYLINDER 7600. 0 0.0015 0.00965 360 0.03 0.04305783910328 330

# TRES RAPIDE  
#GRID\_SIZE 4 4 4  
# RAPIDE  
GRID\_SIZE 8 17 14  
# LENT  
#GRID\_SIZE 8 65 40

### L sector

## Inner part

OUTER\_FILLET 2810.8 0.029 0.101496 -0.002865 0.01 -11.2499 146.2503  
CYLINDER 2810.8 0.029 0.04 0.101496 22.4998 0 -0.002865 146.2503  
CYLINDER 2810.8 0.029 0.04 0.101493 22.4998 0 -0.002868 168.7501  
CYLINDER 2810.8 0.029 0.04 0.101491 22.4998 0 -0.002865 191.2499  
CYLINDER 2810.8 0.029 0.04 0.101492 22.4998 0 -0.002865 213.7497  
OUTER\_FILLET 2810.8 0.029 0.101492 -0.002865 0.01 11.2499 213.7497

## Middle part

CYLINDER 2810.8 0.04 0.071997 0.104346 22.4998 0 0 146.2503  
CYLINDER 2810.8 0.04 0.071997 0.104365 22.4998 0 0 168.7501  
CYLINDER 2810.8 0.04 0.071997 0.104370 22.4998 0 0 191.2499  
CYLINDER 2810.8 0.04 0.071997 0.104365 22.4998 0 0 213.7497

## Outer part

CYLINDER 2810.8 0.071997 0.103982 0.03478102989088 22.5006 0 0.03478102989088 146.2491  
CYLINDER 2810.8 0.071997 0.103980 0.03478102989088 22.4998 0 0 146.2503  
CYLINDER 2810.8 0.071997 0.103978 0.03478102989088 22.4990 0 -0.03478102989088 146.2515

CYLINDER 2810.8 0.071997 0.103997 0.0347860296077 22.5006 0 0.0347860296077 168.7497  
CYLINDER 2810.8 0.071997 0.104002 0.0347860296077 22.4998 0 0 168.7501  
CYLINDER 2810.8 0.071997 0.104008 0.0347860296077 22.4990 0 -0.0347860296077 168.7505

CYLINDER 2810.8 0.071997 0.103997 0.034785029664 22.5006 0 0.034785029664 191.2503  
CYLINDER 2810.8 0.071997 0.104002 0.034785029664 22.4998 0 0 191.2499  
CYLINDER 2810.8 0.071997 0.104003 0.034785029664 22.4990 0 -0.034785029664 191.2495

CYLINDER 2810.8 0.071997 0.103977 0.03478002994752 22.5006 0 0.03478002994752 213.7509  
CYLINDER 2810.8 0.071997 0.103980 0.03478002994752 22.4998 0 0 213.7497  
CYLINDER 2810.8 0.071997 0.103978 0.03478002994752 22.4990 0 -0.03478002994752 213.7485

### R sector

## Inner part

OUTER\_FILLET 2810.8 0.029 0.101493 -0.002844 0.01 11.2490 33.7375  
CYLINDER 2810.8 0.029 0.04 0.101493 22.4980 0 -0.002844 33.7375  
CYLINDER 2810.8 0.029 0.04 0.101491 22.4980 0 -0.002846 11.2394  
CYLINDER 2810.8 0.029 0.04 0.101488 22.4980 0 -0.002849 348.7414  
CYLINDER 2810.8 0.029 0.04 0.101490 22.4980 0 -0.002847 326.2434  
OUTER\_FILLET 2810.8 0.029 0.101490 -0.002847 0.01 -11.2490 326.2434

## Middle part

CYLINDER 2810.8 0.04 0.071997 0.104335 22.4980 0 0 33.7375  
CYLINDER 2810.8 0.04 0.071997 0.104332 22.4980 0 0 11.2394  
CYLINDER 2810.8 0.04 0.071997 0.104337 22.4980 0 0 348.7414

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CYLINDER 2810.8 0.04 0.071997 0.104345 22.4980 0 0 326.2434

## Outer part

CYLINDER 2810.8 0.071997 0.103973 0.0347750302307 22.4969 0 0.0347750302307 33.7357

CYLINDER 2810.8 0.071997 0.103970 0.0347750302307 22.4980 0 0 33.7375

CYLINDER 2810.8 0.071997 0.103971 0.0347750302307 22.4992 0 -0.0347750302307 33.7392

CYLINDER 2810.8 0.071997 0.103993 0.0347760301741 22.4969 0 0.0347760301741 11.2389

CYLINDER 2810.8 0.071997 0.103990 0.0347760301741 22.4980 0 0 11.2394

CYLINDER 2810.8 0.071997 0.103993 0.0347760301741 22.4992 0 -0.0347760301741 11.2400

CYLINDER 2810.8 0.071997 0.103988 0.0347780300608 22.4969 0 0.0347780300608 348.7420

CYLINDER 2810.8 0.071997 0.103982 0.0347780300608 22.4980 0 0 348.7414

CYLINDER 2810.8 0.071997 0.103991 0.0347780300608 22.4992 0 -0.0347780300608 348.7409

CYLINDER 2810.8 0.071997 0.103958 0.0347790300041600 22.4969 0 0.0347790300041600 326.2451

CYLINDER 2810.8 0.071997 0.103957 0.0347790300041600 22.4980 0 0 326.2434

CYLINDER 2810.8 0.071997 0.103968 0.0347790300041600 22.4992 0 -0.0347790300041600 326.2417

### GENERAL PARAMETERS

STEP 22.5 16

ARM\_LENGTH 3000

SIGNAL 3