

# Characteristics of the rotor R4-05 for the O4 NCal system VIR-0859A-22

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## 1 Introduction

This note follows the same discussion made on the rotor R4-01 in [VIR-0591C-22](#). The drawings and figures of the rotor can be found in this technical note.

The rotor has been engraved IPHC-R4-05 on one side and sandblasted on the other side.

## 2 Measurement method

To determine the geometry of the rotor we will use the same method as for R4-01 (see [VIR-0591C-22](#)). The thickness was measured using  $24 \times 2 = 48$  points (see fig. 1), the outer diameter was measured in  $4 \times 2 = 8$  points and the inner diameter using 4 points.

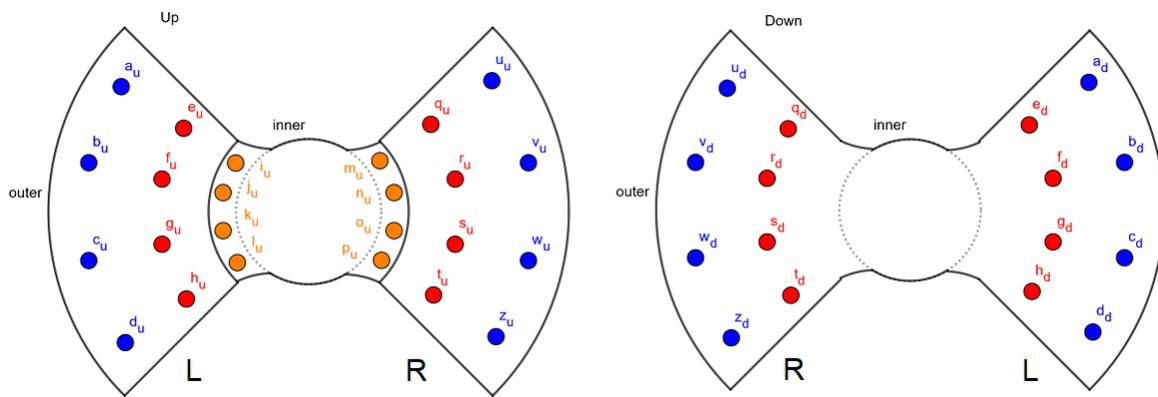


Figure 1: Outline of the faces of the rotor with the measurement points. Left figure is face up, right figure is face down. Sectors have been labelled L for left sector and R for right sector.

The tool used to measure the thickness and the outer diameter is a measuring column "Garant 44 5350\_600 HC1" (see [VIR-0160A-22](#)) with a given precision of  $1.8 + L/600 \mu\text{m}$  (L the measured length in mm). A vernier caliper "TESA-CAL IP67" with a precision of  $20 \mu\text{m}$  was used to measure the inner diameter.

The measuring column was operated on a different metrology table than the first rotor, different measurements were made to check the flatness on a surface roughly equivalent to the rotor layout. The value range from 0 to  $2 \mu\text{m}$ . The rms of the 16 values is  $0.9 \mu\text{m}$ .

### 2.1 Thermal effects and density

The rotors R4-05, R4-06, R4-07 and R4-31 have been machined from a different aluminum block than R4-01, R4-02, R4-03 and R4-04. Following the same process as in [VIR-0160A-22](#) (see fig. 2), we made similar measurements on a reference cylinder engraved R4-TEMOIN-2022 (see fig. 3) coming from this new aluminum block (see table 1).

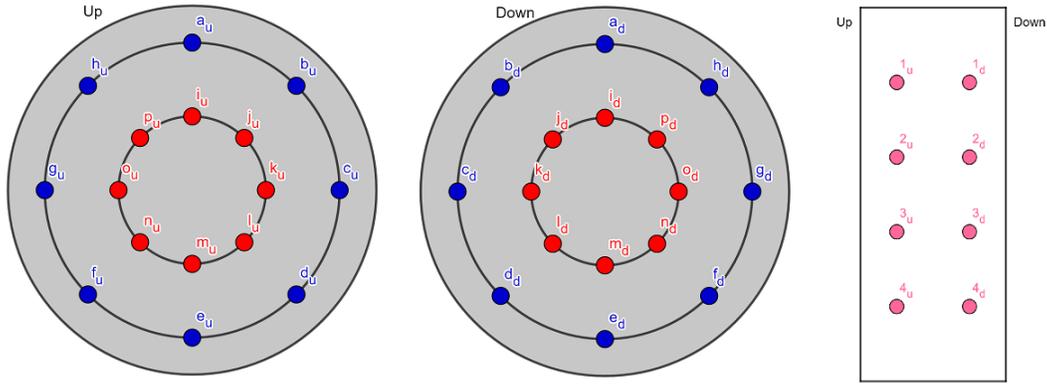


Figure 2: Outline of the faces and side of the reference cylinder, colored dots represent where the measures are taken. From left to right, face up, face down, side. The radius of the red inner points is  $r_{red}=43.54$  mm and the radius of the blue outer points is  $r_{blue}=86.08$  mm.

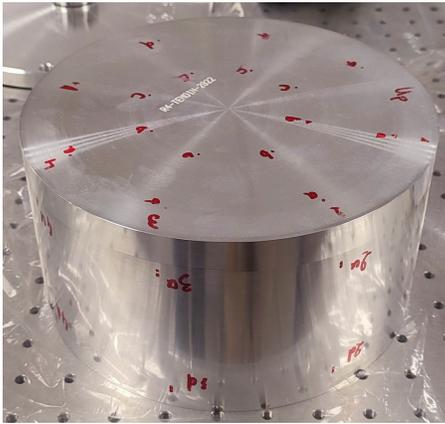


Figure 3: Picture of the up face and side of R4-TEMOIN-2022.

Measurements	Column 1 (21.2°C)	Column 2 (21.35°C)
Mean diameter (mm)	210.028	210.023
Mean height (mm)	109.864	109.865
m (kg)	10.6998	
$\rho$ (kg.m <sup>-3</sup> )	2811.0	2811.2
$\rho_{23^\circ\text{C}}$ (kg.m <sup>-3</sup> )	2810.8	

Table 1: Measurements made at IPHC on R4-TEMOIN-2022. A weight of 0.5 is applied on the inner points for the height. The mean density of the cylinder at 23.5°C is shown in yellow.

The density computed at 23°C is then  $2810.8 \pm 0.2$  kg.m<sup>-3</sup> for R4-05. This density is measured in air, if the rotor is used under vacuum, the density should be increased by the air density ( $\rho_{air}=1.3$  kg.m<sup>-3</sup>).

### 3 Raw measurements of the rotor

This section presents the raw measurements made on the rotor at the ambient temperature of 22.1°C. Table 2 shows the thickness measurements according to the measurement points defined in figure 1. The rotor is laying on the table. The rotor surface as well as the table are not perfectly flat. Some space could be present in between that should be subtracted when computing the rotor thickness as discussed later.

Measurement point	L sector		Measurement point	R sector	
	Up	Down		Up	Down
a	104.425	104.409	q	104.406	104.409
b	104.427	104.427	r	104.409	104.412
c	104.451	104.444	s	104.414	104.419
d	104.450	104.456	t	104.428	104.433
e	104.453	104.432	u	104.374	104.368
f	104.451	104.441	v	104.380	104.382
g	104.458	104.448	w	104.394	104.400
h	104.466	104.458	z	104.415	104.413
i	101.612		m	101.614	
j	101.609		n	101.612	
k	101.609		o	101.612	
l	101.610		p	101.612	

Table 2: Raw measurements of the height in mm for each point at 22.1°C on L and R sectors of R4-05.

Table 3 displays the diameter measurements. The measurements were made on 4\*2 diameters (two parts of each diameter, the up and down sides of the rotor).

Measurement point	Up	Down
1	207.944	207.891
2	207.957	207.916
3	207.958	207.899
4	207.949	207.875

Table 3: Raw measurements of the diameter in mm for each point at 22.1°C on R4-05.

Theoretical values were taken for the inner radius  $r_{\min} = 29$  mm and the up face radius for the counterweight  $r_{\text{counterweight}} = 40$  mm (see drawing in [VIR-0591C-22](#)).

## 4 Extracting the geometrical parameters

### 4.1 Thickness

We need to correct the possible gap between the rotor and the measuring table. Assuming that the table is flatter than the rotor surface we can extract the gap from the measurement of the top surface considering the plane tangents to the highest points (asking them to be on both sectors). For this rotor these points are g, h, t for the up and d, h, t for the down face (see fig. 1). Using the measurements in table 2 we can compute a plane equation for each side of the rotor in cartesian coordinates:

$$\text{Up plane equation : } z = -4.10 \times 10^{-4}x - 5.64 \times 10^{-4}y + 104.43 \quad (1)$$

$$\text{Down plane equation : } z = -2.66 \times 10^{-4}x + 5.13 \times 10^{-4}y + 104.46 \quad (2)$$

Using eqs. (1) and (2) the gap can be determined, see table 4. The maximum rms of the gap for each sector is 31  $\mu\text{m}$ .

Measurement point	L sector		Measurement point	R sector	
	Up	Down		Up	Down
a	7	97	q	-13	56
b	28	66	r	-8	40
c	23	32	s	-1	22
d	37	0	t	0	0
e	-22	58	u	-2	99
f	-5	41	v	4	65
g	0	22	w	10	30
h	0	0	z	12	4

Table 4: Gap computed in  $\mu\text{m}$  on up and down sides of both sectors of R4-05.

We can then compute the rotor thickness for each point by removing these gaps. If one of the raw values is lower than the corrected thickness we take this lowest value. The value of each point is shown in table 5 at 23°C.

Measurement point	L sector	Measurement point	R sector
a	104.411	q	104.395
b	104.429	r	104.403
c	104.446	s	104.415
d	104.452	t	104.430
e	104.433	u	104.370
f	104.443	v	104.382
g	104.450	w	104.396
h	104.460	z	104.415
i	101.614	m	101.616
j	101.611	n	101.614
k	101.611	o	101.614
l	101.612	p	101.614

Table 5: Measurements of the thickness in mm for each point at 23°C on L and R sectors of R4-05.

## 4.2 Radius

Using comparators while the rotor is rotating on its axis we can determine the deformation on both sectors and compute different radii values. Table 6 shows the raw measurements using comparators on L and R sectors. The measurements were made on the up, center and down sides of L and R sectors using three comparators for a total of  $5 \times 3 \times 2 = 30$  points (the first and last points are near the edge of the sectors).

Measurement point	L sector			R sector		
	Up	Center	Down	Up	Center	Down
A	0	0	0	0	10	-5
B	30	45	40	30	40	30
C	35	55	45	30	50	40
D	20	50	35	20	40	40
E	-10	15	0	-25	5	5

Table 6: Raw measurements in  $\mu\text{m}$  of the comparators for the L and R sectors of R4-05.

The zeroing of the comparators was made arbitrarily close to the edge of the sector. The offsets shown in table 6 are measured relative to this reference.

To compute the radius per measurement point we use the following process: First we compute the mean deformation for one comparator. Then we remove this mean deformation to each measurement of this comparator. The corrected shift value is added to the mean radius of 103.964 mm computed using table 3 at 23°C. This process is repeated for each comparator. The final radius for each point are shown in table 7.

Measurement point	L sector			R sector		
	Up	Center	Down	Up	Center	Down
A	103.949	103.931	103.939	103.949	103.941	103.934
B	103.979	103.976	103.979	103.979	103.971	103.969
C	103.984	103.986	103.984	103.979	103.981	103.979
D	103.969	103.981	103.974	103.969	103.971	103.979
E	103.939	103.946	103.939	103.924	103.936	103.944

Table 7: Radius measurements in mm at 22.1°C for the L and R sectors of R4-05.

## 5 Characterization of the rotor using a simple model

### 5.1 Theoretical model of the rotor

As explained in VIR-0591C-22 the theoretical strain of the mirror at  $2f$  using FROMAGE v1r2 with the rotor design parameters:

$$\text{strain}(2f) = \frac{2.1217 \times 10^{-18}}{(2f_{rot})^2}$$

This strain value will be compared to models based on the measurements of the rotor.

### 5.2 Thickness

A simple model can be used to determine a mean value for the thickness and its uncertainty.

As shown on fig. 1, a total of 16 points were used to compute the thickness of each sector. In this case we will not consider the inner points so that we obtain uniform sectors.

For the simple model we take the thickness as the mean value of table 5: 104.421 mm at 23°C. Since we have a limited number of measurement points, to be conservative we take the thickness uncertainty as the rms of table 5 (26.6  $\mu\text{m}$ ) to which we add linearly the metrology table uncertainty (0.9  $\mu\text{m}$ ) and the tool uncertainty (2.0  $\mu\text{m}$ ). Therefore, for this simple model, the thickness is  $104.421 \pm 0.030$  mm.

### 5.3 Radius

For the simple model we take the radius as the mean value of table 7: 103.964 mm at 23°C. Using a linear sum of the rms of table 7 (19.8  $\mu\text{m}$ ) and the tool uncertainty (2.2  $\mu\text{m}$ ) we take an uncertainty of 22  $\mu\text{m}$  on the mean radius.

We have to point out that we do not take into account the fact that the sectors might not be centered on the same axis. Therefore the uncertainty might be underestimated. We will then consider each sector individually later.

### 5.4 Expected NCal signal and uncertainties

The geometry used to describe the rotor as a simple model is represented in figure 4.

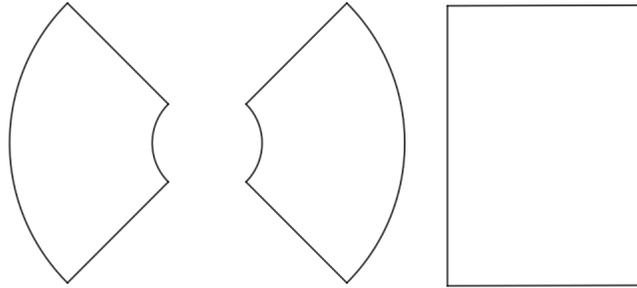


Figure 4: Simple model geometry used to describe the rotor. Left is a front view, right is a side view.

Using the analytical equation of the strain at 2f (see eq.8 in [Newtonian calibrator tests during the Virgo O3 data taking](#)) we compute with our parameters ( $d = 1.7$  m and an angle  $\phi = 34.7^\circ$ ):

$$\text{strain}(2f) = \frac{2.1192 \times 10^{-18}}{(2f_{rot})^2}.$$

Using FROMAGE on this geometry we compute the following 2f strain on the mirror at a distance of 1.7m and an angle of 34.7°:

$$\text{strain}(2f) = \frac{2.1193 \times 10^{-18}}{(2f_{rot})^2}$$

Comparing the theoretical model strain with the simple model at 2f using FROMAGE we obtain a relative deviation of 0.113%.

Comparing the analytical strain at 2f with FROMAGE we obtain a relative deviation of 0.005%.

The uncertainties considered for this model are displayed in table 8.

R4-05 rotor parameter simple model (23°C)			NCal 2f signal uncertainty	
name	value	uncertainty	formula	value (%)
Density $\rho$ (kg.m <sup>-3</sup> )	2810.8	0.2	$\delta\rho/\rho$	0.007
Thickness $b$ (mm)	104.421	$3.0 \times 10^{-2}$	$\delta b/b$	0.028
$r_{max}$ (mm)	103.964	$2.2 \times 10^{-2}$	$4\delta r_{max}/r_{max}$	0.085
$G$ (m <sup>3</sup> .kg <sup>-1</sup> .s <sup>-2</sup> )	$6.67430 \times 10^{-11}$	$1.5 \times 10^{-15}$	$\delta G/G$	0.002
Temperature $T$ (°C)	23	3	$\frac{\partial h}{\partial T} \frac{\Delta T}{h}$	0.014
Total uncertainty from the rotor (quadratic sum)				0.091

Table 8: Uncertainties on the amplitude of the calibration signal at 2f from the R4-05 rotor simple model geometry. The uncertainties from the opening angles are not included.

## 6 Characterization of the rotor using an advanced model

### 6.1 Thickness

A more advanced model can be used considering the deformations on the surfaces of the sectors for better accuracy. Each measurement point of table 5 can be considered as a sub-sector with its own thickness.

The uncertainty on this value is more complex to evaluate. As a conservative approach we use the maximum rms of the deviation to a plane for each sector (31  $\mu\text{m}$  see section 4.1) to which we add linearly the uncertainty on the flatness of the measurement table (0.9  $\mu\text{m}$ ) as well as the measurement tool (2.0  $\mu\text{m}$ ). The total uncertainty on the thickness is 34  $\mu\text{m}$ .

### 6.2 Radius

On fig. 1 we divided the external sectors in 4 sub-sectors for each sector (blue points). We convert the point of table 7 to the grid of fig. 1 by averaging the two closest values and converting them to 23°C. The results are shown in table 9. We notice that the L sector is on average 3  $\mu\text{m}$  larger than the R sector.

Radius	L sector			R sector		
	Up	Center	Down	Up	Center	Down
1	103.966	103.956	103.961	103.966	103.958	103.954
2	103.984	103.983	103.984	103.981	103.978	103.976
3	103.979	103.986	103.981	103.976	103.978	103.981
4	103.956	103.966	103.959	103.949	103.956	103.964

Table 9: Radius measurements (in mm at 23°C) for the L and R sectors of R4-05.

The maximum rms of the radii for each sector is 12.1  $\mu\text{m}$ . The tool uncertainty is 2.2  $\mu\text{m}$ . Like for the thickness we use a linear sum and find the uncertainty on both radii to be 14  $\mu\text{m}$ .

### 6.3 Counterweight

A counterweight has been designed to reduce the unbalance of the rotor. This counterweight is made of aluminum 2017 ( $\rho_{\text{Al}_{2017}} = 2790 \text{ kg.m}^{-3}$ ) and the geometry is shown in fig. 5.

The dimensions of the counterweight are: an inner radius of 10 mm, an outer radius of 40 mm and a material cut with a chord of 54.70 mm to balance the rotor (see hatched area on fig. 5).

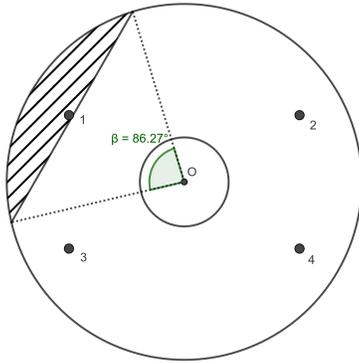


Figure 5: Outline of the counterweight for R4-05. The hatched area represents the material removed.

## 6.4 Expected NCal signals and uncertainties

### 6.4.1 Advanced geometry including chamfers and counterweight

The geometry used to describe the rotor as an advanced model is represented in figure 6. The external parts of the sectors are divided in 3 sub-sectors each to correspond to the different radii determined. In addition we include the counterweight, the screws and screw holes.

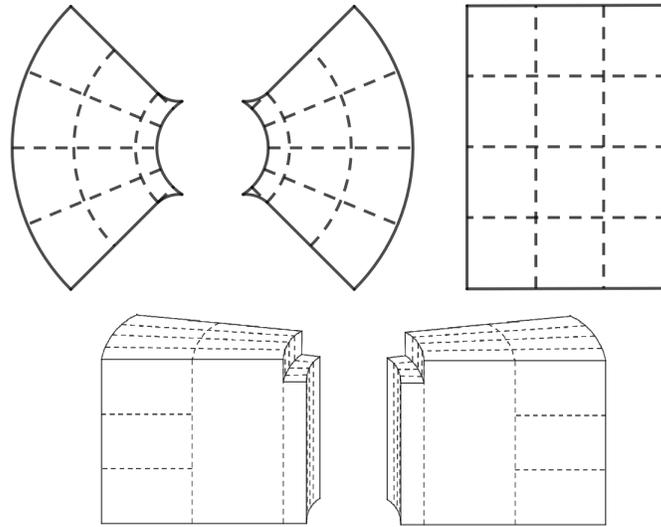


Figure 6: Advanced model geometry used to describe the rotor. Top left is a front view, top right is a side view (external sub-sectors) and bottom is a tilted view of the sectors. Only the 4 external part sectors are divided in 3 sub-sectors each. The chamfers are visible on the inner radius.

Using FROMAGE on this geometry gives the following strains:

- $\text{strain}(1f) = \frac{1.4458 \times 10^{-20}}{(1f_{rot})^2}$
- $\text{strain}(2f) = \frac{2.1187 \times 10^{-18}}{(2f_{rot})^2}$

$$\bullet \text{ strain}(3f) = \frac{3.1629 \times 10^{-23}}{(3f_{rot})^2}$$

The relative deviation to the simple model at 2f is 0.028%.

### 6.4.2 Remaining geometry uncertainty

Since R4-02 and following have been machined with a better precision than R4-01 as seen from the lower 1f value. The remaining geometry uncertainties are taking as for R4-01.

### 6.4.3 Uncertainties

To set an uncertainty on the strain(2f) from the description of the geometry we take the difference between the simple model ( $\text{strain}(2f) = 2.1193 \times 10^{-18}/(2f)^2$ ) and the advanced model ( $\text{strain}(2f) = 2.1187 \times 10^{-18}/(2f)^2$ ). This deviation, 0.028%, is reported in table 10 as modelling uncertainty.

The uncertainties considered for this full model are displayed in table 10.

R4-05 rotor parameter advanced model (23°C)			NCal 2f signal uncertainty	
name	mean value	uncertainty	formula	value (%)
Density $\rho$ (kg.m <sup>-3</sup> )	2810.8	0.2	$\delta\rho/\rho$	0.007
Thickness $b$ left sector (12 sub-sectors) (mm)	104.441	$3.4 \times 10^{-2}$	$\delta b/b$	0.032
Thickness $b$ right sector (12 sub-sectors) (mm)	104.401			
$r_{max}$ left sector (12 ext sub-sectors) (mm)	103.971	$1.4 \times 10^{-2}$	$4\delta r_{max}/r_{max}$	0.055
$r_{max}$ right sector (12 ext sub-sectors) (mm)	103.968			
$G$ (m <sup>3</sup> .kg <sup>-1</sup> .s <sup>-2</sup> )	$6.67430 \times 10^{-11}$	$1.5 \times 10^{-15}$	$\delta G/G$	0.002
Temperature $T$ (°C)	23	3	$\left  \frac{\partial h}{\partial T} \right  \frac{\Delta T}{h}$	0.014
Modelling uncertainty				0.028
FROMAGE grid uncertainty				0.005
Opening angle and sector asymmetry uncertainty				$< 5 \times 10^{-4}$
Remaining geometry uncertainty				$< 5 \times 10^{-4}$
Total uncertainty from the rotor (quadratic sum)				0.071

Table 10: Uncertainties on the amplitude of the calibration signal at 2f from the R4-05 rotor advanced model geometry at 23°C.

## A Appendix

```
### This is a cfg file for a more realistic geometry of the mirror and the Virgo NCal R4-05 (2022)
```

```
### ALL THE OBJECTS ARE DEFINED IN THE MIRROR'S FRAME (0,x,y,z),
### with 0 the center of the mirror, x axis along the ITF's beam toward the beam-splitter,
### y axis orthogonal to x in the plane of the ITF,
### z axis orthogonal to the plane of the ITF upward
```

```
### MIRROR DEFINITION
```

```
GRID_SIZE 12 30 8
```

```
CYLINDER 2202. 0 0.175 0.2 360 0 0 0
```

```
GRID_SIZE 1 1 1
```

```
# Defining the flats on the edge of the mirror
```

```
CUT_CYL 2202. 0.175 0.2 0.05 0 0
```

```
CUT_CYL 2202. 0.175 0.2 0.05 0 180
```

```
# Defining the ears and anchors of the mirror
```

```
CUBOID 2202. 0.090 0.010 0.015 0 0.1782 -0.0125
```

```
CUBOID 2202. 0.090 0.010 0.015 0 -0.1782 -0.0125
```

```
CUBOID 2202. 0.039 0.008 0.008 -0.02 -0.1772 -0.024
```

```
CUBOID 2202. 0.039 0.008 0.008 -0.02 0.1772 -0.024
```

```
CUBOID 2202. 0.039 0.008 0.008 0.02 -0.1772 -0.024
```

```
CUBOID 2202. 0.039 0.008 0.008 0.02 0.1772 -0.024
```

```
### ROTOR DEFINITION: CYLINDER DENSITY INNER_RADIUS OUTER_RADIUS THICKNESS OPEN_ANGLE r z theta
```

```
ROTOR_CYLINDRICAL 1.7 34.7 0 0
```

```
### COUNTERWEIGHT 2790.
```

```
GRID_SIZE 16 65 40
```

```
CYLINDER 2790. 0.010 0.040 0.003 360 0 0.049513 0
```

```
GRID_SIZE 1 1 1
```

```
CUT_CYL 2790. 0.040 0.003 0.05470 0 150
```

```
### SCREW HOLES
```

```
GRID_SIZE 4 4 4
```

```
CYLINDER -2810.9 0 0.0015 0.012 360 0.03 0.04480707911944 150
```

```
CYLINDER -2810.9 0 0.0015 0.012 360 0.03 0.0448060790982 30
```

```
CYLINDER -2810.9 0 0.0015 0.012 360 0.03 0.04480807914068 210
```

```
CYLINDER -2810.9 0 0.0015 0.012 360 0.03 0.04480707911944 330
```

```
### SCREWS COUNTERWEIGHT
```

```
CYLINDER 4810. 0 0.0015 0.003 360 0.03 0.0495134428908685 150
```

```
CYLINDER 7600. 0 0.0015 0.00665 360 0.03 0.04415807914068 150
```

```
CYLINDER 4810. 0 0.0015 0.003 360 0.03 0.0495134428908685 30
```

```
CYLINDER 7600. 0 0.0015 0.00665 360 0.03 0.04415807914068 30
```

```
CYLINDER 4810. 0 0.0015 0.003 360 0.03 0.0495134428908685 210
```

```
CYLINDER 7600. 0 0.0015 0.00665 360 0.03 0.04415807914068 210
```

```
CYLINDER 4810. 0 0.0015 0.003 360 0.03 0.0495134428908685 330
CYLINDER 7600. 0 0.0015 0.00665 360 0.03 0.04415807914068 330

# TRES RAPIDE
#GRID_SIZE 4 4 4
# RAPIDE
#GRID_SIZE 8 17 14
# LENT
GRID_SIZE 8 65 40

### L sector

## Inner part
OUTER_FILLET 2810.9 0.029 0.101614 -0.002832 0.01 -11.25 146.25
CYLINDER 2810.9 0.029 0.04 0.101614 22.5 0 -0.002832 146.25
CYLINDER 2810.9 0.029 0.04 0.101611 22.5 0 -0.002835 168.75
CYLINDER 2810.9 0.029 0.04 0.101611 22.5 0 -0.002832 191.25
CYLINDER 2810.9 0.029 0.04 0.101612 22.5 0 -0.002832 213.75
OUTER_FILLET 2810.9 0.029 0.101612 -0.002832 0.01 11.25 213.75

## Middle part
CYLINDER 2810.9 0.04 0.072002 0.104433 22.5 0 0 146.25
CYLINDER 2810.9 0.04 0.072002 0.104443 22.5 0 0 168.75
CYLINDER 2810.9 0.04 0.072002 0.104450 22.5 0 0 191.25
CYLINDER 2810.9 0.04 0.072002 0.104460 22.5 0 0 213.75

## Outer part
CYLINDER 2810.9 0.072002 0.103966 0.03480373921572 22.5 0 0.03480373921572 146.25
CYLINDER 2810.9 0.072002 0.103956 0.03480373921572 22.5 0 0 146.25
CYLINDER 2810.9 0.072002 0.103961 0.03480373921572 22.5 0 -0.03480373921572 146.25

CYLINDER 2810.9 0.072002 0.103984 0.03480973934316 22.5 0 0.03480973934316 168.75
CYLINDER 2810.9 0.072002 0.103983 0.03480973934316 22.5 0 0 168.75
CYLINDER 2810.9 0.072002 0.103984 0.03480973934316 22.5 0 -0.03480973934316 168.75

CYLINDER 2810.9 0.072002 0.103979 0.0348154061301867 22.5 0 0.0348154061301867 191.25
CYLINDER 2810.9 0.072002 0.103986 0.0348154061301867 22.5 0 0 191.25
CYLINDER 2810.9 0.072002 0.103981 0.0348154061301867 22.5 0 -0.0348154061301867 191.25

CYLINDER 2810.9 0.072002 0.103956 0.0348174061726667 22.5 0 0.0348174061726667 213.75
CYLINDER 2810.9 0.072002 0.103966 0.0348174061726667 22.5 0 0 213.75
CYLINDER 2810.9 0.072002 0.103959 0.0348174061726667 22.5 0 -0.0348174061726667 213.75

### R sector

## Inner part
OUTER_FILLET 2810.9 0.029 0.101616 -0.002795 0.01 11.25 33.75
CYLINDER 2810.9 0.029 0.04 0.101616 22.5 0 -0.002795 33.75
CYLINDER 2810.9 0.029 0.04 0.101614 22.5 0 -0.002797 11.25
CYLINDER 2810.9 0.029 0.04 0.101614 22.5 0 -0.002797 348.75
CYLINDER 2810.9 0.029 0.04 0.101614 22.5 0 -0.002797 326.25
OUTER_FILLET 2810.9 0.029 0.101614 -0.002797 0.01 -11.25 326.25

## Middle part
CYLINDER 2810.9 0.04 0.072002 0.104395 22.5 0 0 33.75
CYLINDER 2810.9 0.04 0.072002 0.104403 22.5 0 0 11.25
```

CYLINDER 2810.9 0.04 0.072002 0.104415 22.5 0 0 348.75  
CYLINDER 2810.9 0.04 0.072002 0.104430 22.5 0 0 326.25

## ## Outer part

CYLINDER 2810.9 0.072002 0.103966 0.0347900722587733 22.5 0 0.0347900722587733 33.75  
CYLINDER 2810.9 0.072002 0.103958 0.0347900722587733 22.5 0 0 33.75  
CYLINDER 2810.9 0.072002 0.103954 0.0347900722587733 22.5 0 -0.0347900722587733 33.75

CYLINDER 2810.9 0.072002 0.103981 0.0347940723437333 22.5 0 0.0347940723437333 11.25  
CYLINDER 2810.9 0.072002 0.103978 0.0347940723437333 22.5 0 0 11.25  
CYLINDER 2810.9 0.072002 0.103976 0.0347940723437333 22.5 0 -0.0347940723437333 11.25

CYLINDER 2810.9 0.072002 0.103976 0.03479873910952 22.5 0 0.03479873910952 348.75  
CYLINDER 2810.9 0.072002 0.103978 0.03479873910952 22.5 0 0 348.75  
CYLINDER 2810.9 0.072002 0.103981 0.03479873910952 22.5 0 -0.03479873910952 348.75

CYLINDER 2810.9 0.072002 0.103949 0.0348050725773733 22.5 0 0.0348050725773733 326.25  
CYLINDER 2810.9 0.072002 0.103956 0.0348050725773733 22.5 0 0 326.25  
CYLINDER 2810.9 0.072002 0.103964 0.0348050725773733 22.5 0 -0.0348050725773733 326.25

## ### GENERAL PARAMETERS

STEP 22.5 16

ARM\_LENGTH 3000

SIGNAL 3