# Properties of the binary black hole merger GW150914 

The LIGO Scientific Collaboration and The Virgo Collaboration (compiled 11 February 2016)


#### Abstract

On September 14, 2015, the Laser Interferometer Gravitational-wave Observatory (LIGO) detected a gravitational-wave transient (GW150914); we characterise the properties of the source and its parameters. The data around the time of the event were analysed coherently across the LIGO network using a suite of accurate waveform models that describe gravitational waves from a compact binary system in general relativity. GW150914 was produced by a nearly equal mass binary black hole of masses $36_{-4}^{+5} \mathrm{M}_{\odot}$ and $29_{-4}^{+4} \mathrm{M}_{\odot}$ (for each parameter we report the median value and the range of the $90 \%$ credible interval). The dimensionless spin magnitude of the more massive black hole is bound to be $<0.7$ (at $90 \%$ probability). The luminosity distance to the source is $410_{-180}^{+160} \mathrm{Mpc}$, corresponding to a redshift $0.09_{-0.04}^{+0.03}$ assuming standard cosmology. The source location is constrained to an annulus section of $590 \mathrm{deg}^{2}$, primarily in the southern hemisphere. The binary merges into a black hole of mass $62_{-4}^{+4} \mathrm{M}_{\odot}$ and spin $0.67_{-0.07}^{+0.05}$. This black hole is significantly more massive than any other known in the stellar-mass regime.


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Introduction- In Ref. [1] we reported the detection of gravitational waves (GWs), observed on September 14, 2015 at 09:50:45 UTC by the twin instruments of the Laser Interferometer Gravitational-wave Observatory (LIGO) located at Hanford, Washington, and Livingston, Louisiana, in the USA [2, 3]. The transient signal, named GW150914, was detected with a false-alarm-probability of $<2 \times 10^{-7}$ and has been associated with the merger of a binary system of black holes (BHs).

Here we discuss the properties of this source and its inferred parameters. The results are based on a complete analysis of the data surrounding this event. The only information from the search-stage is the time of arrival of the signal. Crucially, this analysis differs from the search in the following fundamental ways: it is coherent across the LIGO network, it uses waveform models that include the full richness of the physics introduced by BH spins, and it covers the full multidimensional parameter space of the considered models with a fine (stochastic) sampling; we also account for uncertainty in the calibration of the measured strain.

In general relativity, two objects in orbit slowly spiral together due to the loss of energy and momentum through gravitational radiation [4, 5]. This is in contrast to Newtonian gravity where bodies can follow closed, elliptical orbits [6, 7]. As the binary shrinks, the frequency and amplitude of the emitted GWs increase. Eventually the two objects merge. If these objects are BHs, they form a single perturbed BH that radiates GWs at a constant frequency and exponentially damped amplitude as it settles to its final state [8, 9].

An isolated BH is described by only its mass and spin, since we expect the electric charge of astrophysical BHs to be negligible [10-13]. Merging binary black holes (BBHs) are therefore relatively simple systems. The two BHs are described by eight intrinsic parameters: the masses $m_{1,2}$ and spins $\boldsymbol{S}_{1,2}$ (magnitude and orientation) of the individual BHs. For a BH of mass $m$, the spin can be at most
$G m^{2} / c$; hence it is conventional to quote the dimensionless spin magnitude $a=c|\boldsymbol{S}| /\left(G m^{2}\right) \leq 1$. Nine additional parameters are needed to fully describe the binary: the location (luminosity distance $D_{\mathrm{L}}$, right ascension $\alpha$ and declination $\delta$ ); orientation (the binary's orbital inclination $\iota$ and polarization $\psi$ ); time $t_{\mathrm{c}}$ and phase $\phi_{\mathrm{c}}$ of coalescence, and the eccentricity (two parameters) of the system.

Radiation reaction is efficient in circularising orbits [14] before the signal enters the sensitive frequency band of the instruments. In our analysis, we assume circular orbits (we therefore do not include the eccentricity parameters), and we find no evidence for residual eccentricity, see the Discussion. Under the approximation of a circular orbit, dominant emission from the binary occurs at twice the orbital frequency [15].

The gravitational waveform observed for GW150914 comprises $\sim 10$ cycles during the inspiral phase from 30 Hz , followed by the merger and ringdown. The properties of the binary affect the phase and amplitude evolution of the observed GWs allowing us to to measure the source parameters. Here we briefly summarise these signatures, and provide an insight into our ability to characterise the properties of GW150914 before we present the details of the Results; for methodological studies, we refer the reader to [16-21] and references therein.

In general relativity, gravitational radiation is fully described by two independent, and time-dependent polarizations, $h_{+}$and $h_{\times}$. Each instrument $k$ measures the strain

$$
\begin{equation*}
h_{k}=F_{k}^{(+)} h_{+}+F_{k}^{(\times)} h_{\times}, \tag{1}
\end{equation*}
$$

a linear combination of the polarisations weighted by the antenna beam patterns $F_{k}^{(+, \times)}(\alpha, \delta, \psi)$, which depend on the source location in the sky and the polarisation of the waves [22, 23]. During the inspiral and at the leading order, the GW polarizations can be expressed as

$$
\begin{align*}
& h_{+}(t)=A_{\mathrm{GW}}(t)\left(1+\cos ^{2} \iota\right) \cos \phi_{\mathrm{GW}}(t),  \tag{2a}\\
& h_{\times}(t)=-2 A_{\mathrm{GW}}(t) \cos \iota \sin \phi_{\mathrm{GW}}(t), \tag{2b}
\end{align*}
$$

where $A_{\mathrm{GW}}(t)$ and $\phi_{\mathrm{GW}}(t)$ are the GW amplitude and phase, respectively. For a binary viewed face-on, GWs are circularly polarized, whereas for a binary observed edgeon, GWs are linearly polarized.

During the inspiral, the phase evolution $\phi_{\mathrm{GW}}\left(t ; m_{1,2}, \boldsymbol{S}_{1,2}\right) \quad$ can be computed using postNewtonian (PN) theory, which is a perturbative expansion in powers of the orbital velocity $v / c$ [24]. For GW150914, $v / c$ is in the range $\approx 0.2-0.5$ in the LIGO sensitivity band. At the leading order, the phase evolution is driven by a particular combination of the two masses, commonly called the chirp mass [25],

$$
\begin{equation*}
\mathcal{M}=\frac{\left(m_{1} m_{2}\right)^{3 / 5}}{M^{1 / 5}} \simeq \frac{c^{3}}{G}\left[\frac{5}{96} \pi^{-8 / 3} f^{-11 / 3} \dot{f}\right]^{3 / 5} \tag{3}
\end{equation*}
$$

where $f$ is the GW frequency, $\dot{f}$ is its time derivative and $M=m_{1}+m_{2}$ is the total mass. Additional parameters enter at each of the following PN orders. First, the mass ratio, $q=m_{2} / m_{1} \leq 1$, and the BH spin components parallel to the orbital angular momentum vector $L$ affect the phase evolution. The full degrees of freedom of the spins enter at higher orders. Thus, from the inspiral, we expect to measure the chirp mass best and only place weak constraints on the mass ratio and (the components parallel to $L$ of) the spins of the BHs [18, 26].

Spins are responsible for an additional characteristic effect: if misaligned with respect to $L$, they cause the binary's orbital plane to precess around the almost-constant direction of the total angular momentum of the binary, $\boldsymbol{J}=\boldsymbol{L}+\boldsymbol{S}_{1}+\boldsymbol{S}_{2}$. This leaves characteristic amplitude and phase modulations in the observed strain [27], as $\psi$ and $\iota$ become time-dependent. The size of these modulations depends crucially on the viewing angle of the source.

As the BHs get closer to each other and their velocities increase, the accuracy of the PN expansion degrades, and eventually the full solution of Einstein's equations is needed to accurately describe the binary evolution. This is accomplished using numerical relativity (NR) which, after the initial breakthrough [28--30], has been improved continuously to achieve the sophistication of modeling needed for our purposes. The details of the merger and ringdown are primarily governed by the mass and spin of the final BH . In particular, the final mass and spin determine the (constant) frequency and decay time of the BH's ringdown to its final state [31]. The late stage of the coalescence allows us to measure the total mass which, combined with the measurement of the chirp mass and mass-ratio from the early inspiral, yields estimates of the individual component masses for the binary.

The observed frequency of the signal is redshifted by a factor of $(1+z)$, where $z$ is the cosmological redshift. There is no intrinsic mass or length scale in vacuum general relativity, and the dimensionless quantity that incorporates frequency is $f G m / c^{3}$. Consequently, a redshifting of frequency is indistinguishable from a rescaling of the
masses by the same factor [32, 33]. We therefore measure redshifted masses $m$, which are related to source frame masses by $m=(1+z) m^{\text {source }}$. However, the GW amplitude $A_{\mathrm{GW}}$, Eq. (2), also scales linearly with the mass and is inversely proportional to the comoving distance in an expanding universe. This implies that $A_{\mathrm{GW}} \propto 1 / D_{\mathrm{L}}$ and from the GW signal alone we can directly measure the luminosity distance, but not the redshift.

The observed time delay, and the need for the registered signal at the two sites to be consistent in amplitude and phase, allow us to localize the source to a ring on the sky [34, 35]. Where there is no precession, changing the viewing angle of the system simply changes the observed waveform by an overall amplitude and phase. Furthermore, the two polarizations are the same up to overall amplitude and phase. Thus, for systems with minimal precession, the distance, binary orientation, phase at coalescence and sky location of the source change the overall amplitude and phase of the source in each detector, but they do not change the signal morphology. Phase and amplitude consistency allow us to untangle some of the geometry of the source. If the binary is precessing, the GW amplitude and phase have a complicated dependency on the orientation of the binary, which provides additional information.

Our ability to characterise GW150914 as the signature of a binary system of compact objects, as we have outlined above, is dependent on the finite signal-to-noise ratio of the signal and the specific properties of the underlying source. These properties described in detail below, and the inferred parameters for GW150914 are summarised in Table I and Figures 166

Method-Full information about the properties of the source is provided by the probability density function (PDF) $p(\vec{\vartheta} \mid \vec{d})$ of the unknown parameters, given the two data-streams from the instruments $\vec{d}$.

The posterior PDF is computed through a straightforward application of Bayes' theorem [36, 37]. It is proportional to the product of the likelihood of the data given the parameters $\mathcal{L}(\vec{d} \mid \vec{\vartheta})$, and the prior PDF on the parameters $p(\vec{\vartheta})$ before we consider the data. From the (marginalised) posterior PDF, shown in Figures $1-5$ for selected parameters, we then construct credible intervals for the parameters, reported in Table I

In addition, we can compute the evidence $\mathcal{Z}$ for the model under consideration. The evidence (also known as marginal likelihood) is the average of the likelihood under the prior on the unknown parameters for a specific model choice.

At the detector output we record the data $d_{k}(t)=$ $n_{k}(t)+h_{k}^{\mathrm{M}}(t ; \vec{\vartheta})$, where $n_{k}$ is the noise, and $h_{k}^{\mathrm{M}}$ is the measured strain, which differs from the physical strain $h_{k}$ from Eq. (1) as a result of the detectors' calibration [38]. In the frequency domain, we model the effect of calibra-
tion uncertainty by considering

$$
\begin{align*}
\tilde{h}_{k}^{\mathrm{M}}(f ; \vec{\vartheta})= & \tilde{h}_{k}(f ; \vec{\vartheta})\left[1+\delta A_{k}(f ; \vec{\vartheta})\right] \\
& \times \exp \left[i \delta \phi_{k}(f ; \vec{\vartheta})\right] \tag{4}
\end{align*}
$$

where $\delta A_{k}(f ; \vec{\vartheta})$ and $\delta \phi_{k}(f ; \vec{\vartheta})$ are the frequencydependent amplitude and phase calibration-error functions, respectively. These calibration-error functions are modelled using a cubic spline polynomial, with five nodes per spline model placed uniformly in $\ln f$ [39].

We have analyzed the data at the time of this event using a coherent analysis. Under the assumption of stationary, Gaussian noise uncorrelated in each detector [40], the likelihood function for the LIGO network is [17, 41]:
$\mathcal{L}(\vec{d} \mid \vec{\vartheta}) \propto \exp \left[-\frac{1}{2} \sum_{k=1,2}\left\langle h_{k}^{\mathrm{M}}(\vec{\vartheta})-d_{k} \mid h_{k}^{\mathrm{M}}(\vec{\vartheta})-d_{k}\right\rangle\right]$,
where $\langle\cdot \mid \cdot\rangle$ is the noise-weighted inner product [17]. We model the noise as a stationary Gaussian process of zero mean and known variance, which is estimated from the power spectrum computed using up to 1024 s of data adjacent to, but not containing, the GW signal [41].

The source properties are encoded into the two polarizations $h_{+}$and $h_{\times}$. Here we focus on the case in which they originate from a compact binary coalescence; we use model waveforms (described below) that are based on solving Einstein's equations for the inspiral and merger of two BHs.

The computation of marginalized PDFs and the model evidences require the evaluation of multi-dimensional integrals. This is addressed by using a suite of Bayesian parameter-estimation and model-selection algorithms tailored to this problem [41]. We verify the results by using two independent stochastic sampling engines based on Markov-chain Monte Carlo [42, 43] and nested sampling [44, 45] techniques ${ }^{1}$

In addition to this analysis, we consider a model which is not derived from a particular physical scenario and makes minimal assumptions about $h_{+, \times}$. In this case we compute directly the posterior $p(\vec{h} \mid \vec{d})$ by reconstructing $h_{+, \times}$ using a linear combination of elliptically polarized sineGaussian wavelets whose amplitudes are assumed to be consistent with a uniform source distribution [46], see Figure 6. The number of wavelets in the linear combination is not fixed a priori but is optimized via Bayesian model selection. This analysis directly infers the PDF of the GW strain given the data, $p(\vec{h} \mid \vec{d})$.

[^0]BBH waveform models- For the modelled analysis of binary coalescences, an accurate waveform prediction for the gravitational radiation $h_{+, x}$ is essential. As a consequence of the complexity of solving the two body problem in general relativity, several techniques have to be combined to describe all stages of the binary coalescence. While the early inspiral is well described by the analytical PN expansion [47], which relies on small velocities and weak gravitational fields, the strong-field merger stage can only be solved in full generality by large-scale NR simulations [28-40]. Since these pioneering works, numerous improvements have enabled numerical simulations of BBHs with sufficient accuracy for the applications considered here and for the region of parameter space of relevance to GW150914 (see, e.g. [48-50]). Tremendous progress has also been made in the past decade to combine analytical and numerical approaches, and now several accurate waveform models are available, and they are able to describe the entire coalescence for a large variety of possible configurations [49, 51-57]. Extending and improving such models is an active area of research, and none of the current models can capture all possible physical effects (eccentricity, higher order gravitational modes in the presence of spins, etc.) for all conceivable binary systems. We discuss the current state of the art below.

In the Introduction, we outlined how the binary parameters affect the observable GW signal, and now we discuss in the BH spins greater detail. There are two main effects that the BH spins $S_{1}$ and $\boldsymbol{S}_{2}$ have on the phase and amplitude evolution of the GW signal. The spin projections along the direction of the orbital angular momentum $\hat{\boldsymbol{L}}$ affect the inspiral rate of the binary. In particular, spin components aligned (antialigned) with $\hat{\boldsymbol{L}}$ increase (decrease) the number of orbits from any given separation to merger with respect to the nonspinning case [47, 58]. Given the limited signal-to-noise ratio of the observed signal, it is difficult to untangle the full degrees of freedom of the individual BH's spins, see e.g., [59, 60]. However, some spin information is encoded in a dominant spin effect. Several possible 1dimensional parametrizations of this effect can be found in the literature [18, 61, 62]; here, we use a simple massweighted linear combination of the spins [63, 64]

$$
\begin{equation*}
\chi_{\mathrm{eff}}=\frac{c}{G}\left(\frac{\boldsymbol{S}_{1}}{m_{1}}+\frac{\boldsymbol{S}_{2}}{m_{2}}\right) \cdot \frac{\hat{\boldsymbol{L}}}{M} \tag{6}
\end{equation*}
$$

which takes values between -1 (both BHs have maximal spins antialigned with respect to the orbital angular momentum) and +1 (maximal aligned spins).

Having described the effect of the two spin components aligned with the orbital angular momentum, four in-plane spin components remain. These lead to precession of the spins and the orbital plane, which in turn introduces modulations in the strain amplitude and phase as measured at the detectors. At leading order in the PN expansion, the
equations that describe precession in a BBH are [27]

$$
\begin{align*}
\dot{\boldsymbol{L}} & =\frac{G}{c^{2} r^{3}}\left(B_{1} \boldsymbol{S}_{1 \perp}+B_{2} \boldsymbol{S}_{2 \perp}\right) \times \boldsymbol{L}  \tag{7}\\
\dot{\boldsymbol{S}}_{i} & =\frac{G}{c^{2} r^{3}} B_{i} \boldsymbol{L} \times \boldsymbol{S}_{i} \tag{8}
\end{align*}
$$

where $\boldsymbol{S}_{i \perp}$ is the component of the spin perpendicular to $\boldsymbol{L} ; r$ is the orbital separation; $B_{1}=2+3 q / 2$ and $B_{2}=2+3 /(2 q)$, and $i=\{1,2\}$. It follows from (7) and (8) that $\hat{\boldsymbol{L}}$ and $\hat{\boldsymbol{S}}_{i}$ precess around the almost-constant direction of the total angular momentum $J$. For a nearly equal-mass binary (as we find is the case for GW150914), the precession angular frequency can be approximated by $\Omega_{\mathrm{p}} \approx 7 G J /\left(c^{2} r^{3}\right)$, and the total angular momentum is dominated during the inspiral by the orbital contribution, $J \approx L$. Additional, higher order spin-spin interactions can also contribute significantly to precession effects for some comparable-mass binaries [65, 66].

The in-plane spin components rotate within the orbital plane at different velocities. Because of nutation of the orbital plane, the magnitude of the in-plane spin components oscillates around a mean value, but those oscillations are typically small. To first approximation, one can quantify the level of precession in a binary by averaging over the relative in-plane spin orientation. This is achieved by the following effective precession spin parameter [67]

$$
\begin{equation*}
\chi_{\mathrm{p}}=\frac{c}{B_{1} G m_{1}^{2}} \max \left(B_{1} S_{1 \perp}, B_{2} S_{2 \perp}\right)>0 \tag{9}
\end{equation*}
$$

where $\chi_{\mathrm{p}}=0$ corresponds to an aligned-spin (nonprecessing) system, and $\chi_{\mathrm{p}}=1$ to a binary with the maximum level of precession. Although the definition of $\chi_{\mathrm{p}}$ is motivated by configurations that undergo many precession cycles during inspiral, we find that it is also a good approximate indicator of the in-plane spin contribution for the late inspiral and merger of GW150914.

For the analysis of GW150914, we consider waveform models constructed within two frameworks capable of accurately describing the GW signal in the parameter space of interest. The effective-one-body (EOB) formalism [68-72] combines perturbative results from the weak-field PN approximation with strong-field effects from the test-particle limit. These results are resummed in a suitable Hamiltonian, radiation-reaction force and gravitational polarizations, and are improved by calibrating (unknown) higherorder PN terms to NR simulations. Henceforth, we use "EOBNR" to indicate waveforms within this formalism. Waveform models that include spin effects have been developed, for both double non-precessing spins [52, 57] (11 independent parameters) and double precessing spins [53] ( 15 independent parameters). Here, we report results using the non-precessing model [52] tuned to NR simulations [73]. This model is formulated as a set of differential equations that are computationally too expensive to solve for the millions of likelihood evaluations required
for the analysis. Therefore, a frequency-domain reducedorder model [74, 75] was implemented that faithfully represents the original model with an accuracy that is better than the statistical uncertainty caused by the instruments' noise ${ }^{2}$ Bayesian analyses that use the double precessing spin model [53] are more time consuming and are not yet finalized. The results will be fully reported in a future publication.

An alternative inspiral-merger-ringdown phenomenological formalism [76-78] is based on extending frequency-domain PN expressions and hybridizing PN and EOB with NR waveforms. Henceforth, we use "IMRPhenom" to indicate waveforms within this formalism. Several waveform models that include aligned-spin effects have been constructed within this approach [56, 63, 64], and here we employ the most recent model based on a fitting of untuned EOB waveforms [52] and NR hybrids [55, 56] of non-precessing systems. To include leadingorder precession effects, aligned-spin waveforms are rotated into precessing waveforms [79]. Although this model captures some two-spin effects, it was principally designed to accurately model the waveforms with respect to an effective spin parameter similar to $\chi_{\text {eff }}$ above. The dominant precession effects are introduced through a lower-dimensional effective spin description [67, 80], motivated by the same physical arguments as the definition of $\chi_{\mathrm{p}}$. This provides us with an effective-precessing-spin model [80] with 13 independent parameters ${ }^{3}$

All models we use are restricted to non-eccentric inspirals. They also include only the dominant spherical harmonic modes in the non-precessing limit.

Choice of priors- We analyse coherently $T=8 \mathrm{~s}$ of data with a uniform prior on $t_{\mathrm{c}}$ of width of $\pm 0.1 \mathrm{~s}$, centred on the time reported by the online analysis [1, 81], and a uniform prior in $[0,2 \pi]$ for $\phi_{c}$. We consider the frequency region between 20 Hz , below which the sensitivity of the instruments significantly degrades (see panel (b) of Figure 3 in Ref. [1]), and 1024 Hz , a safe value for the highest frequency contribution to radiation from binaries in the mass range considered here.

Given the lack of any additional astrophysical constraints on the source at hand, our prior choices on the parameters are uninformative. We assume sources uniformly distributed in volume, and the orbital orientation priors are uniform on the 2 -sphere. We use uniform priors in $m_{1,2} \in$ $[10,80] \mathrm{M}_{\odot}$, with the constraint that $m_{2} \leq m_{1}$. We use a uniform prior in the spin magnitudes $a_{1,2} \in[0,1]$. For angles subject to change due to precession effects we give values at a reference gravitational-wave frequency $f_{\text {ref }}=20$

[^1]Hz . The priors on spin orientation for the precessing model is uniform on the 2 -sphere. For the non-precessing model, the prior on the spin magnitudes may be interpreted as the dimensionless spin projection onto $\hat{\boldsymbol{L}}$ having a uniform distribution $[-1,1]$. This range includes binaries where the two spins are strongly antialigned relative to one another. Many such antialigned-spin comparable-mass systems are unstable to large-angle precession well before entering our sensitive band [82, 83] and could not have formed from an asymptotically spin antialigned binary. We could exclude those systems if we believe the binary is not precessing. However, we do not make this assumption here and instead accept that the models can only extract limited spin information about a more general, precessing binary.

We also need to specify the prior ranges for the amplitude and phase error functions $\delta A_{k}(f ; \vec{\vartheta})$ and $\delta \phi_{k}(f ; \vec{\vartheta})$. The calibration during the time of observation of GW150914 is characterised by a $1-\sigma$ statistical uncertainty of no more than $10 \%$ in amplitude and $10^{\circ}$ in phase [1, 38]. We use zero-mean Gaussian priors on the values of the spline at each node with widths corresponding to the uncertainties quoted above [39]. Calibration uncertainties therefore add 10 parameters per instrument to the model used in the analysis. For validation purposes we also considered an independent method that assumes frequency-independent calibration errors [84], and obtained consistent results.

Results - The results of the analysis using binary coalescence waveforms are posterior PDFs for the parameters describing the GW signal and the model evidence. A summary is provided in Table $\square$ For the model evidence, we quote (the logarithm of) the Bayes factor $\mathcal{B}_{\mathrm{s} / \mathrm{n}}=\mathcal{Z} / \mathcal{Z}_{\mathrm{n}}$, which is the ratio of the evidence for a coherent signal hypothesis divided by that for (Gaussian) noise [45]. At the leading order, the Bayes factor and the optimal signal-tonoise ratio $\rho=\left[\sum_{k}\left\langle h_{k}^{\mathrm{M}} \mid h_{k}^{\mathrm{M}}\right\rangle\right]^{1 / 2}$ are related by $\ln \mathcal{B}_{\mathrm{s} / \mathrm{n}} \approx$ $\rho^{2} / 2$ [85].

Before discussing parameter estimates in detail, we consider how the inference is affected by the choice of compact-binary waveform model. From Table I, we see that the posterior estimates for each parameter are broadly consistent across the two models, despite the fact that they are based on different analytical approaches and that they include different aspects of BBH spin dynamics. The models' $\log$ Bayes factors, $288.7 \pm 0.2$ and $290.1 \pm 0.2$, are also comparable for both models: the data do not allow us to conclusively prefer one model over the other [88]. Therefore, we use both for the Overall column in Table We combine the posterior samples of both distributions with equal weight, in effect marginalising over our choice of waveform model. These averaged results give our best estimate for the parameters describing GW150914.

In Table $\mathbb{Z}$, we also indicate how sensitive our results are to our choice of waveform. For each parameter, we give systematic errors on the boundaries of the $90 \%$ credible


FIG. 1. Posterior PDFs for the source-frame component masses $m_{1}^{\text {source }}$ and $m_{2}^{\text {source }}$, where $m_{2}^{\text {source }} \leq m_{1}^{\text {source }}$. In the 1-dimensional marginalised distributions we show the Overall (solid black), IMRPhenom (blue) and EOBNR (red) PDFs; the dashed vertical lines mark the $90 \%$ credible interval for the Overall PDF. The 2-dimensional plot shows the contours of the $50 \%$ and $90 \%$ credible regions plotted over a colour-coded posterior density function.
intervals due to the uncertainty in the waveform models considered in the analysis; the quoted values are the $90 \%$ range of a normal distribution estimated from the variance of results from the different models ${ }_{\square}^{4}$ Assuming normally distributed error is the least constraining choice [89] and gives a conservative estimate. The uncertainty from waveform modelling is less significant than statistical uncertainty; therefore, we are confident that the results are robust against this potential systematic error. We consider this point in detail later in the paper.

The analysis presented here yields an optimal coherent signal-to-noise ratio of $\rho=25.1_{-1.7}^{+1.7}$. This value is higher than the one reported by the search [1, 3] because it is obtained using a finer sampling of (a larger) parameter space.

GW150914's source corresponds to a stellar-mass BBH with individual source-frame masses $m_{1}^{\text {source }}=36_{-4}^{+5} \mathrm{M}_{\odot}$ and $m_{2}^{\text {source }}=29_{-4}^{+4} \mathrm{M}_{\odot}$, as shown in Table $I$ and Figure 1 .

[^2]TABLE I. Summary of the parameters that characterise GW150914. For model parameters we report the median value as well as the range of the symmetric $90 \%$ credible interval [86]; where useful, we also quote $90 \%$ credible bounds. For the logarithm of the Bayes factor for a signal compared to Gaussian noise we report the mean and its $90 \%$ standard error from 4 parallel runs with a nested sampling algorithm [45]. The source redshift and source-frame masses assume standard cosmology [87]. The spin-aligned EOBNR and precessing IMRPhenom waveform models are described in the text. Results for the effective precession spin parameter $\chi_{\mathrm{p}}$ used in the IMRPhenom model are not shown as we effectively recover the prior; we constrain $\chi_{\mathrm{p}}<0.81$ at $90 \%$ probability, see left panel of Figure 5 . The Overall results are computed by averaging the posteriors for the two models. For the Overall results we quote both the $90 \%$ credible interval or bound and an estimate for the $90 \%$ range of systematic error on this determined from the variance between waveform models.

|  | EOBNR | IMRPhenom | Overall |
| :---: | :---: | :---: | :---: |
| Detector-frame total mass $M / \mathrm{M}_{\odot}$ | $70.3_{-4.8}^{+5.3}$ | $70.7_{-4.0}^{+3.8}$ | $70.5_{-4.5 \pm 1.0}^{+4.6 \pm 0.9}$ |
| Detector-frame chirp mass $\mathcal{M} / \mathrm{M}_{\odot}$ | $30.2_{-1.9}^{+2.5}$ | $30.5_{-1.8}^{+1.7}$ | $30.3_{-1.9 \pm 0.4}^{+2.1 \pm 0.4}$ |
| Detector-frame primary mass $m_{1} / \mathrm{M}_{\odot}$ | $39.4{ }_{-4.9}^{+5.5}$ | $38.3_{-3.5}^{+5.5}$ | $38.8{ }_{-4.1 \pm 0.3}^{+5.6 \pm 0.9}$ |
| Detector-frame secondary mass $m_{2} / \mathrm{M}_{\odot}$ | $30.9{ }_{-4.4}^{+4.8}$ | $32.22_{-5.0}^{+3.6}$ | $31.6{ }_{-4.9 \pm 0.6}^{+4.2 \pm 0.1}$ |
| Detector-frame final mass $M_{\mathrm{f}} / \mathrm{M}_{\odot}$ | $67.1_{-4.4}^{+4.6}$ | $67.4_{-3.6}^{+3.4}$ | $67.3_{-4.0 \pm 0.9}^{+4.1 \pm 0.8}$ |
| Source-frame total mass $M^{\text {source }} / \mathrm{M}_{\odot}$ | $65.0{ }_{-4.4}^{+5.0}$ | $64.6{ }_{-3.5}^{+4.1}$ | $64.8{ }_{-3.9 \pm 0.5}^{+4.6 \pm 1.0}$ |
| Source-frame chirp mass $\mathcal{M}^{\text {source }} / \mathrm{M}_{\odot}$ | $27.9_{-1.8}^{+2.3}$ | $27.9_{-1.6}^{+1.8}$ | $27.9_{-1.7 \pm 0.2}^{+2.1 \pm 0.4}$ |
| Source-frame primary mass $m_{1}^{\text {source }} / \mathrm{M}_{\odot}$ | $36.3_{-4.5}^{+5.3}$ | $35.1_{-3.3}^{+5.2}$ | $35.7_{-3.8 \pm 0.0}^{+5.4 \pm 1.1}$ |
| Source-frame secondary mass $m_{2}^{\text {source }} / \mathrm{M}_{\odot}$ | $28.6_{-4.2}^{+4.4}$ | $29.5{ }_{-4.5}^{+3.3}$ | $29.1{ }_{-4.4 \pm 0.5}^{+3.8 \pm 0.2}$ |
| Source-fame final mass $M_{\mathrm{f}}^{\text {source }} / \mathrm{M}_{\odot}$ | $62.0_{-4.0}^{+4.4}$ | $61.6_{-3.1}^{+3.7}$ | $61.8_{-3.5 \pm 0.4}^{+4.2 \pm 0.9}$ |
| Mass ratio $q$ | $0.79_{-0.19}^{+0.18}$ | $0.84{ }_{-0.21}^{+0.14}$ | $0.82_{-0.21 \pm 0.03}^{+0.16 \pm 0.01}$ |
| Effective inspiral spin parameter $\chi_{\text {eff }}$ | $-0.09_{-0.17}^{+0.19}$ | $-0.03_{-0.15}^{+0.14}$ | $-0.06_{-0.18 \pm 0.07}^{+0.17 \pm 0.01}$ |
| Dimensionless primary spin magnitude $a_{1}$ | $0.32_{-0.28}^{+0.45}$ | $0.31{ }_{-0.27}^{+0.51}$ | $0.31-0.28 \pm 0.01$ |
| Dimensionless secondary spin magnitude $a_{2}$ | $0.57_{-0.51}^{+0.40}$ | $0.39_{-0.34}^{+0.50}$ | $0.46{ }_{-0.42 \pm 0.01}^{+0.48 \pm 0.07}$ |
| Final spin $a_{\text {f }}$ | $0.67{ }_{-0.08}^{+0.06}$ | $0.67{ }_{-0.05}^{+0.05}$ | $0.67{ }_{-0.07 \pm 0.03}^{+0.05 \pm 00}$ |
| Luminosity distance $D_{\mathrm{L}} / \mathrm{Mpc}$ | $390_{-180}^{+170}$ | $440_{-180}^{+140}$ | $410_{-180 \pm \pm 0}^{+160 \pm 20}$ |
| Source redshift $z$ | $0.083_{-0.036}^{+0.033}$ | $0.093_{-0.036}^{+0.028}$ | $\begin{aligned} & 0.088_{-0.038 \pm 0.009}^{+0.031 \pm 0.004} \\ & \hline \end{aligned}$ |
| Upper bound on primary spin magnitude $a_{1}$ | 0.65 | 0.71 | $0.69 \pm 0.05$ |
| Upper bound on secondary spin magnitude $a_{2}$ | 0.93 | 0.81 | $0.88 \pm 0.10$ |
| Lower bound on mass ratio $q$ | 0.64 | 0.67 | $0.65 \pm 0.03$ |
| Log Bayes factor $\ln \mathcal{B}_{\mathrm{s} / \mathrm{n}}$ | $288.7 \pm 0.2$ | $290.1 \pm 0.2$ | - |

The two BHs are nearly equal mass. We bound the mass ratio to the range $0.65 \leq q \leq 1$ with $90 \%$ probability. For comparison, the highest observed neutron star mass is $2.01 \pm 0.04 \mathrm{M}_{\odot}$ [90], and the conservative upper-limit for the mass of a stable neutron star is $3 \mathrm{M}_{\odot}$ [91, 92]. The masses inferred from GW150914 are an order of magnitude larger than these values, which implies that these two compact objects of GW150914 are BHs, unless exotic alternatives, e.g., boson stars [93], do exist. This result establishes the presence of stellar-mass BBHs in the Universe. It also proves that BBHs formed in Nature can merge within an Hubble time [94].

To convert the masses measured in the detector frame to physical source-frame masses, we required the redshift of the source. As discussed in the Introduction, GW observations are directly sensitive to the luminosity distance to a
source, but not the redshift [95]. We find that GW150914 is at $D_{\mathrm{L}}=410_{-180}^{+160} \mathrm{Mpc}$. Assuming a flat $\Lambda \mathrm{CDM}$ cosmology with Hubble parameter $H_{0}=67.9 \mathrm{~km} \mathrm{~s}^{-1} \mathrm{Mpc}^{-1}$ and matter density parameter $\Omega_{\mathrm{m}}=0.306$ [87], the inferred luminosity distance corresponds to a redshift of $z=$ $0.09_{-0.04}^{+0.03}$.

The luminosity distance is strongly correlated to the inclination of the orbital plane with respect to the line of sight [17]. For precessing systems, the orientation of the orbital plane is time-dependent. We therefore describe the source inclination by $\theta_{J N}$, the angle between the total angular momentum (which typically is approximately constant throughout the inspiral) and the line of sight, and we quote its value at a reference gravitational-wave frequency $f_{\text {ref }}=20 \mathrm{~Hz}$. The posterior PDF shows that an orientation of the total orbital angular momentum of the BBH strongly


FIG. 2. Posterior PDFs for the source luminosity distance $D_{\mathrm{L}}$ and the binary inclination $\theta_{J N}$. In the 1-dimensional marginalised distributions we show the Overall (solid black), IMRPhenom (blue) and EOBNR (red) PDFs; the dashed vertical lines mark the $90 \%$ credible interval for the Overall PDF. The 2-dimensional plot shows the contours of the $50 \%$ and $90 \%$ credible regions plotted over a colour-coded PDF.
misaligned to the line of sight is disfavoured; the probability that $45^{\circ}<\theta_{J N}<135^{\circ}$ is 0.35 .

The masses and spins of the BHs in a (circular) binary are the only parameters needed to determine the final mass and spin of the BH that is produced at the end of the merger. Appropriate relations are embedded intrinsically in the waveform models used in the analysis, but they do not give direct access to the parameters of the remnant BH . However, applying the fitting formula calibrated to nonprecessing NR simulations provided in [96] to the posterior for the component masses and spins [97], we infer the mass and spin of the remnant BH to be $M_{\mathrm{f}}^{\text {source }}=62_{-4}^{+4} \mathrm{M}_{\odot}$, and $a_{\mathrm{f}}=0.67_{-0.07}^{+0.05}$, as shown in Figure 3 and Table I These results are fully consistent with those obtained using an independent non-precessing fit [55]. The systematic uncertainties of the fit are much smaller than the statistical uncertainties. The value of the final spin is a consequence of conservation of angular momentum in which the total angular momentum of the system (which for a nearly equal mass binary, such as GW150914's source, is dominated by the orbital angular momentum) is converted partially into the spin of the remnant black hole and partially radiated away in GWs during the merger. Therefore, the final spin is more precisely determined than either of the spins of the binary's BHs.

The calculation of the final mass also provides an esti-


FIG. 3. PDFs for the source-frame mass and spin of the remnant BH produced by the coalescence of the binary. In the 1-dimensional marginalised distributions we show the Overall (solid black), IMRPhenom (blue) and EOBNR (red) PDFs; the dashed vertical lines mark the $90 \%$ credible interval for the Overall PDF. The 2-dimensional plot shows the contours of the $50 \%$ and $90 \%$ credible regions plotted over a colour-coded PDF.
mate of the total energy emitted in GWs. GW150914 radiated a total of $3.0_{-0.5}^{+0.5} \mathrm{M}_{\odot} c^{2}$ in GWs, the majority of which was at frequencies in LIGO's sensitive band. These values are fully consistent with those given in the literature for NR simulations of similar binaries [98, 99]. The energetics of a BBH merger can be estimated at the order of magnitude level using simple Newtonian arguments. The total energy of a binary system at separation $r$ is given by $E \approx\left(m_{1}+m_{2}\right) c^{2}-G m_{1} m_{2} /(2 r)$. For an equal-mass system, and assuming the inspiral phase to end at about $r \approx 5 G M / c^{2}$, then around $2-3 \%$ of the initial total energy of the system is emitted as GWs. Only a fully general relativistic treatment of the system can accurately describe the physical process during the final strong-field phase of the coalescence. This indicates that a comparable amount of energy is emitted during the merger portion of GW150914, leading to $\approx 5 \%$ of the total energy emitted.

We further infer the peak GW luminosity achieved during the merger phase by applying to the posteriors a separate fit to non-precessing NR simulations [100]. The source reached a maximum instantaneous GW luminosity of $3.6_{-0.4}^{+0.5} \times 10^{56} \mathrm{erg} \mathrm{s}^{-1}=200_{-20}^{+30} \mathrm{M}_{\odot} c^{2} / \mathrm{s}$. Here, the uncertainties include an estimate for the systematic error of the fit as obtained by comparison with a separate set of precessing NR simulations, in addition to the dominant statistical contribution. An order-of-magnitude estimate of the luminosity corroborates this result. For the dominant


FIG. 4. An orthographic projection of the PDF for the sky location of GW150914 showing contours of the $50 \%$ and $90 \%$ credible regions plotted over a colour-coded PDF. The sky localization forms part of an annulus, set by the time delay of $6.9_{-0.4}^{+0.5} \mathrm{~ms}$ between the Livingston and Hanford detectors.
mode, the flux can be estimated by $\approx c^{3}|\dot{h}|^{2} /(16 \pi G) \sim$ $10^{5} \mathrm{erg} \mathrm{s}^{-1} \mathrm{~m}^{-2}$, where we use a GW amplitude of $|h| \approx$ $10^{-21}$ at a frequency of 250 Hz [1]. Using the inferred distance leads to an estimated luminosity of $\sim 10^{56} \mathrm{erg} \mathrm{s}^{-1}$. For comparison, the ultraluminous GRB 110918A reached a peak isotropic-equivalent luminosity of $(4.7 \pm 0.2) \times$ $10^{54} \mathrm{erg} \mathrm{s}^{-1}$ [101].

GW ground-based instruments are all-sky monitors with no intrinsic spatial resolution capability for transient signals. A network of instruments is needed to reconstruct the location of a GW in the sky, via time-of-arrival, and amplitude and phase consistency across the network [102]. The observed time-delay of GW150914 between the Livingston and Hanford observatories was $6.9_{-0.4}^{+0.5} \mathrm{~ms}$. With only the two LIGO instruments in observational mode, GW150914's source location can only be reconstructed to approximately an annulus set to first approximation by this time-delay [103, 104]. Figure 4 shows the sky map for GW150914: it corresponds to a projected 2dimensional credible region of $140 \mathrm{deg}^{2}$ ( $50 \%$ probability) and $590 \mathrm{deg}^{2}$ ( $90 \%$ probablity). The associated 3 -dimensional comoving volume probability region is $\sim$ $10^{-2} \mathrm{Gpc}^{3}$; for comparison the comoving density of Milky Way-equivalent galaxies is $\sim 10^{7} \mathrm{Gpc}^{-3}$. This area of the sky was targeted by follow-up observations covering radio, optical, near infra-red, X-ray, and gamma-ray wavelengths that are discussed in [105]; searches for coincident neutrinos are discussed in [106].

Spins are a fundamental property of BHs. Additionally,
their magnitude and orientation with respect to the orbital angular momentum carry an imprint of the evolutionary history of a binary that could help in identifying the formation channel, such as distinguishing binaries formed in the field from those produced through captures in dense stellar environments [94]. The observation of GW150914 allows us for the first time to put direct constraints on BH spins. The EOBNR and IMRPhenom models yield consistent values for the magnitude of the individual spins, see Table $I$. The spin of the primary BH is constrained to $a_{1}<0.7$ (at $90 \%$ probability), and strongly disfavours the primary BH being maximally spinning. The bound on the secondary BH's spin is $a_{2}<0.9$ (at $90 \%$ probability), which is consistent with the bound derived from the prior.

Results for precessing spins are derived using the IMRPhenom model. Spins enter the model through the two effective spin parameters $\chi_{\text {eff }}$ and $\chi_{\mathrm{p}}$. The left panel of Figure 5 shows that despite the short duration of the signal in band we meaningfully constrain $\chi_{\text {eff }}=-0.06_{-0.18}^{+0.17}$, see Table I. The inspiral rate of GW150914 is therefore only weakly affected by the spins. We cannot, however, extract additional information on the other spin components associated with precession effects. The data are uninformative: the posterior PDF on $\chi_{p}$ (left panel of Figure 5 ) is broadly consistent with the prior, and the distribution of spins (right panel of Figure 5) matches our expectations once the information that $\left|\chi_{\text {eff }}\right|$ is small has been included. Two elements may be responsible for this. If precession occurs, at most one modulation cycle would be present in the LIGO sensitivity window. If the source was viewed with $\boldsymbol{J}$ close to the line-of-sight (Figure 2), the amplitude of possible modulations in the recorded strain is suppressed.

The joint posterior PDFs of the magnitude and orientation of $\boldsymbol{S}_{1}$ and $\boldsymbol{S}_{2}$ are shown in the right panel of Figure 5 . The angle of the spins with respect to $\hat{L}$ (the tilt angle) is considered a tracer of BBH formation channels [94]. However, we can place only weak constraints on this parameter for GW150914: the probabilities that $\hat{\boldsymbol{S}}_{1}$ and $\hat{\boldsymbol{S}}_{2}$ are at an angle between $45^{\circ}$ and $135^{\circ}$ with respect to the normal to the orbital plane $\hat{\boldsymbol{L}}$ are 0.78 and 0.79 , respectively. For this specific geometrical configuration the spin magnitude estimates are $a_{1}<0.7$ and $a_{2}<0.8$ at $90 \%$ probability.

Some astrophysical formation scenarios favour spins nearly-aligned with the orbital angular momentum, particularly for the massive progenitors that in these scenarios produce GW150914 [94, 107, 108]. To estimate the impact of this prior hypothesis on our interpretation, we used the fraction $(2.5 \%)$ of the spin-aligned result (EOBNR) with $\hat{\boldsymbol{S}}_{1,2} \cdot \hat{\boldsymbol{L}}>0$ to revise our expectations. If both spins must be positively and strictly co-aligned with $\boldsymbol{L}$, then we can constrain the two individual spins at $90 \%$ probability to be $a_{1}<0.2$ and $a_{2}<0.3$.

The loss of linear momentum through GWs produces a recoil of the merger BH with respect to the binary's original centre of mass [109, 110]. The recoil velocity depends


FIG. 5. Left: PDFs (solid black line) for the $\chi_{\mathrm{p}}$ and $\chi_{\text {eff }}$ spin parameters compared to their prior distribution (green line). The dashed vertical lines mark the $90 \%$ credible interval. The 2 -dimensional plot shows probability contours of the prior (green) and marginalised PDF (black). The 2-dimensional plot shows the contours of the $50 \%$ and $90 \%$ credible regions plotted over a colourcoded PDF. Right: PDFs for the dimensionless component spins $c \boldsymbol{S}_{1} /\left(G m_{1}^{2}\right)$ and $c \boldsymbol{S}_{2} /\left(G m_{2}^{2}\right)$ relative to the normal to the orbital plane $\hat{\boldsymbol{L}}$, marginalized over uncertainties in the azimuthal angles. The bins are constructed linearly in spin magnitude and the cosine of the tilt angles $\cos ^{-1}\left(\hat{\boldsymbol{S}}_{i} \cdot \hat{\boldsymbol{L}}\right)$, where $i=\{1,2\}$, and, therefore, by design have equal prior probability.
on the spins (magnitude and orientation) of the BHs of the binary and could produce super-kicks for spins in the orbital plane of the binary [111--113]. Unfortunately, the weak constraints on the spins (magnitude and direction) of GW150914 prevent us from providing a meaningful limit on the kick velocity of the resulting BH .

Finally, we can cast the results into PDFs of the strain at the two instruments $p(\vec{h}(\vec{\vartheta}) \mid \vec{d})$ and compare them to the posterior estimates $p(\vec{h} \mid \vec{d})$ obtained using the minimalassumption wavelet model [81]. The waveforms are shown in Figure 6. There is remarkable agreement between the actual data and the reconstructed waveform under the two model assumptions. As expected, the uncertainty is greater for the minimal-assumption reconstruction due to greater flexibility in its waveform model. The agreement between the reconstructed waveforms using the two models can be quantified through the noise-weighted inner product that enters Eq. (5), and it is found to be $94_{-3}^{+2} \%$, consistent with expectations for the signal-to-noise ratio at which GW150914 was observed.

Discussion- We have presented measurements of the heaviest stellar-mass BHs known to date, and the first stellar-mass BBH. The system merges into a BH of $\approx$ $60 \mathrm{M}_{\odot}$. So far, stellar-mass BHs of masses $\approx 10 \mathrm{M}_{\odot}$ have been claimed using dynamical measurement of Galactic X-ray binaries [114]. Masses as high as $16-20 \mathrm{M}_{\odot}$ and $21-35 \mathrm{M}_{\odot}$ have been reported for IC10 X-1 [115, 116] and NGC300 X-1 [117], respectively; however, these mea-
surements may have been contaminated by stellar winds as discussed in [118] and references therein. Our results attest that BBHs do form and merge within a Hubble time. We have constrained the spin of the primary BH of the binary to be $a_{1}<0.7$ and we have inferred the spin of the remnant BH to be $a_{\mathrm{f}} \approx 0.7$. Up to now, spin estimates of BH candidates have relied on modelling of accretion disks to interpret spectra of X-ray binaries [119]. In contrast, GW measurements rely only on the predictions of general relativity for vacuum spacetime. Further astrophysical implications of these results are discussed in [94, 120].

The statistical uncertainties with which we have characterised the source properties and parameters, reflect the finite signal-to-noise ratio of the observation of GW150914 and the error budget of the strain calibration process. The latter degrades primarily the estimate of the source location. If we assume that the strain was perfectly calibrated, i.e. $h^{\mathrm{M}}=h$, see Eqs. (1) and 4), the $50 \%$ and $90 \%$ credible regions for sky location would become $48 \mathrm{deg}^{2}$ and $150 \mathrm{deg}^{2}$, compared to the actual results of $140 \mathrm{deg}^{2}$ and $590 \mathrm{deg}^{2}$, respectively. The physical parameters show only small changes with the marginalisation over calibration uncertainty, for example, the final mass $M_{\mathrm{f}}^{\text {source }}$ changes from $62_{-4}^{+4} \mathrm{M}_{\odot}$ including calibration uncertainty to $62_{-3}^{+4} \mathrm{M}_{\odot}$ assuming perfect calibration, and the final spin $a_{\mathrm{f}}$ changes from $0.67_{-0.07}^{+0.05}$ to $0.67_{-0.05}^{+0.04}$. The effect of calibration uncertainty is to increase the overall parameter range at given probability, but the medians of the PDFs


FIG. 6. Time-domain data (sampled at 2048 Hz ) and reconstructed waveforms of GW150914, whitened by the noise power spectral density (in Figure 1 of Ref. [1] the data are band-passed and notched filtered), for the H1 (top) and L1 (bottom) detectors. Times are shown relative to September 14, 2015 at 09:50:45 UTC. The ordinate axes on the right are in units of noise standard deviations from zero - i.e. the peak alone is a $\sim 4-\sigma$ excursion relative to the instrument noise at that time - and on the left are normalised in order to preserve the strain amplitude at 200 Hz . The waveforms are plotted as bands representing the uncertainty in the reconstruction. Shaded regions correspond to the $90 \%$ credible regions for the reconstructed waveforms. The broadest (dark blue) shaded region is obtained with the model that does not assume a particular waveform morphology, but instead uses a linear combination of sine-Gaussian wavelets. The lighter, narrower shaded region (cyan) is the result from the modeled analyses using IMRPhenom and EOBNR template waveforms. The thin grey lines are the data. The agreement between the reconstructed waveforms using the two models is found to be $94_{-3}^{+2} \%$.
remain largely unchanged. For GW150914, the dominant source of statistical uncertainty is the finite signal-to-noise ratio. More accurate calibration techniques are currently being tested, and one can expect that in future LIGO observations, the impact of calibration errors on the inference of GW source parameters will be further reduced [38].

Our analysis is based on waveform models that do not include the effect of spins in their full generality. Still, the aligned-spin EOBNR and precessing IMRPhenom models produce consistent results, with an error budget dominated by statistical uncertainty and not systematic errors as evaluated from the physics encoded in these two models. It is, however, important to consider whether additional systematics produced by physics not captured by these models could have affected the results. To this extent, we collected existing numerical waveforms and generated targeted new simulations [121--126]. The simulations were generated with multiple independent codes and sample the posterior region for masses and spins inferred for GW150914. We have added these NR waveforms as 'mock signals' to the data in the neighbourhood of GW150914 and to synthetic data sets representative of LIGO's sensitivity and noise properties at the time of GW150914, with signal-to-noise ratios consistent with the one reported for the actual detec-
tion. We then carried out exactly the same analysis applied to the actual data.

For signals from non-precessing binaries, we recover parameters that are consistent with those describing the mock source. The results obtained with the EOBNR and IMRPhenom model are consistent, which further confirms previous comparison studies of non-precessing models with NR waveforms [52, 56, 127]. For signals that describe precessing binaries, but with orbital angular momentum orientation consistent with the most likely geometry inferred for GW150914, i.e. orbital angular momentum close to aligned or antialigned with the line of sight, we find again that the PDFs are consistent across the models and with the true values of the parameters used for the numerical simulation. For the same physical parameters, but a total angular momentum orientated to give the largest amount of signal modulations at the instrument output, i.e. $\boldsymbol{J}$ approximately perpendicular to the line of sight, the results using the EOBNR and IMRPhenom models do differ from each other. They yield biased and statistically inconsistent PDFs, depending on the specific NR configuration used as the mock signal. This is partly due to the fact that not all physical effects are captured by the models (as in the case of the non-precessing EOBNR model) and partly due to
systematic inaccuracies of the models. The true values of these parameter also lay outside the $90 \%$ credible interval in more than $10 \%$ of the cases. However, we stress that this is not the configuration we find for GW150914.

The outcome of these studies suggests that for GW150914, the results reported here are not appreciably affected by additional waveform systematics beyond those quantified in Table I A detailed analysis will be presented in a forthcoming paper [128]. In addition, we are currently carrying out an analysis using generalized, precessing EOBNR waveforms [53], which depend on the the full 15 independent parameters of a coalescing binary in circular orbit. Preliminary investigations give results that are broadly consistent with those presented here based on the precessing IMRPhenom model, and full details will be reported in the future.

Throughout this work we have considered a model for the binary evolution in the LIGO sensitivity band that assumes a circular orbit. The posterior waveforms according to this model are consistent with minimal-assumption reconstructed waveforms, which make no assumption about eccentricity. Preliminary investigations suggest that eccentricities of $e \lesssim 0.1$ at 10 Hz would not introduce measurable deviations from a circular-orbit signal; however, even larger eccentricities may have negligible effects on the recovered source parameters. At this time, the lack of a model that consistently accounts for the presence of spins and eccentricity throughout the full coalescence prevents us from placing more stringent constraints. We plan to report improved limits in the future.

The analysis reported here is carried out under the assumption that general relativity is correct. The results presented in Figure 6 show no evidence for deviations from the null hypothesis general-relativity model. However, GW150914 provides a new arena for tests of Einstein's theory in unexplored regimes; these are discussed in detail in [129].

Summary- We have reported the properties of GW150914 derived from a coherent analysis of data from the two LIGO detectors, based on the most accurate modelling of the coalescence signal as predicted by general relativity. We have shown that GW150914 originates from a BBH system with component masses $36_{-4}^{+5} \mathrm{M}_{\odot}$ and $29_{-4}^{+4} \mathrm{M}_{\odot}$ at redshift $0.09_{-0.04}^{+0.03}$ that merges to form a BH of mass $62_{-4}^{+4} \mathrm{M}_{\odot}$ and spin $0.67_{-0.07}^{+0.05}$. The final BH is more massive than any other found in the stellar-mass range. We bound the spin magnitude of the binary's primary BH to $<0.7$ (at $90 \%$ probability), and measure the effective spin parameter along the direction of the orbital angular momentum to be $-0.06_{-0.18}^{+0.17}$, but we cannot place meaningful limits on the precession effects. Further implications stemming from our findings are reported in [94, 120, 129]. These results herald the beginning of GW astronomy and provide the first observational insights into the physics of BBHs.

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[^0]:    ${ }^{1}$ The marginalized PDFs and model evidences are computed using the LALInference package of the LIGO Algorithm Library (LAL) software suite available from www.lsc-group.phys.uwm.edu/lal

[^1]:    ${ }^{2}$ In LAL, as well as in technical publications, the aligned, precessing and reduced-order EOBNR models are called SEOBNRv2, SEOBNRv3 and SEOBNRv2_ROM_DoubleSpin, respectively.
    ${ }^{3}$ In LAL, as well as in some technical publications, the model used is called IMRPhenomPv2.

[^2]:    ${ }^{4}$ If $X$ were an edge of a credible interval, we quote systematic uncertainty $\pm 1.64 \sigma_{\text {sys }}$ using the estimate $\sigma_{\mathrm{sys}}^{2}=\left[\left(X_{\mathrm{EOBNR}}-X_{\text {Overall }}\right)^{2}+\right.$ $\left.\left(X_{\text {IMRPhenom }}-X_{\text {Overall }}\right)^{2}\right] / 2$. For parameters with bounded ranges, like the spins, the normal distributions should be truncated. However, for transparency, we still quote the $90 \%$ range of the uncut distributions. These numbers provide estimates of the order of magnitude of the potential systematic error.

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